

A two-scale approximation for wave-wave Interactions in operational wave forecast models

Will Perrie, Bash Toulany, Don Resio and Aron Roland
Bedford Institute of Oceanography
University of North Florida, USA
Tech. Univ. of Darmstadt, Germany



What are the objectives of the project?

1. New wave model using new formulations for efficient quadruplet (nonlinear) wave-wave interactions representation
2. Tests for issues regarding wave transitions: waves and swell, turning winds, shallow water...
3. Tests for real North Atlantic storms

➤ **1: New wave model using new efficient formulations for nonlinear wave physics.**

- **Two-Scale Approximation (TSA)**
- **fetch-limited growth and TSA characteristics**
- **example of hurricane Juan (2003)**

Resio, D., and Perrie, W. 2008: A two-scale approximation for efficient representation of nonlinear energy transfers in a wind wave spectrum. Part 1: Theoretical Development. *J. Phys. Oceanogr.* 38: 2801-2816.

Perrie, W., and Resio, D., 2009: A two-scale approximation for efficient representation of nonlinear energy transfers in a wind wave spectrum. Part 2 Application to observed wave spectra. *J. Phys. Oceanogr.* 39: 2451 – 2476.

Resio, D., C. Long and W. Perrie, 2011: The effect of nonlinear fluxes on spectral shape and energy source-sink balances in wave generation. *J. Phys. Oceanography.* Vol. 41, 782-801.

Perrie, W., B. Toulany, D. Resio, A. Roland, J.-P. Auclair, 2013: A two-scale approximation for wave-wave interactions: Application in an operational wave model. *Ocean Modelling* Vol. 70, 38-51.

Summary

1. Implemented TSA in WW3 and WWM
2. Tests with different source terms: ST1 ~ ST4
3. Reliable results for 'academic' JONSWAP tests
4. " " fetch- and duration-limited growth
5. Turning winds: ongoing test ...
6. N Atlantic tests with hypothetical constant winds
7. Computational efficiency improved
8. Optimization of TSA code is ongoing.

Acknowledgements: Panel on Energy R & D, NOPP ONR.

Wave generation and growth...

a balance equation ...

$$\frac{\partial E(f, \theta)}{\partial t} = -\vec{c}_g \cdot \vec{\nabla} E(f, \theta) + \sum_k S_k(k, \theta)$$

where

\vec{c}_g = group velocity

S_{in} = wind input

S_{ds} = wave dissipation

S_{nl} = nonlinear transfer due to wave-wave interactions

$S_{nl} \Rightarrow$ full Boltzmann Integral - FBI

For internal transfer of wave action (or energy) in the spectrum at n_1 (e.g. at \mathbf{k}_1) via wave-wave interactions by $\mathbf{k}_2, \mathbf{k}_3, \mathbf{k}_4$ - Hasselmann (1962), Zakharov (1966)

$$\frac{\partial n_1}{\partial t} \equiv S_{nl} = \iint T(\mathbf{k}_1, \mathbf{k}_3) d\mathbf{k}_3 \quad \text{where}$$

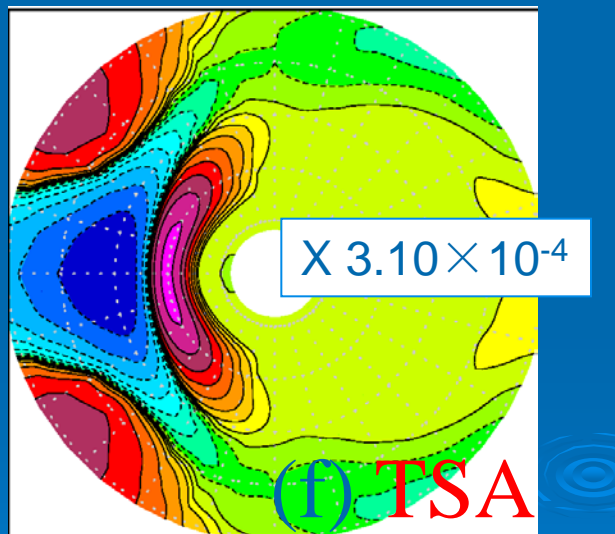
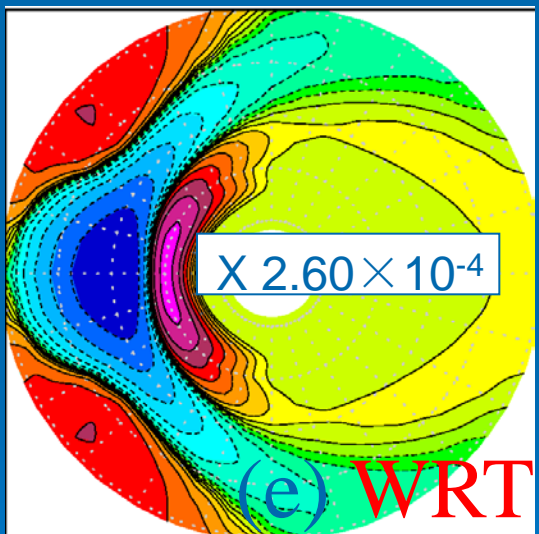
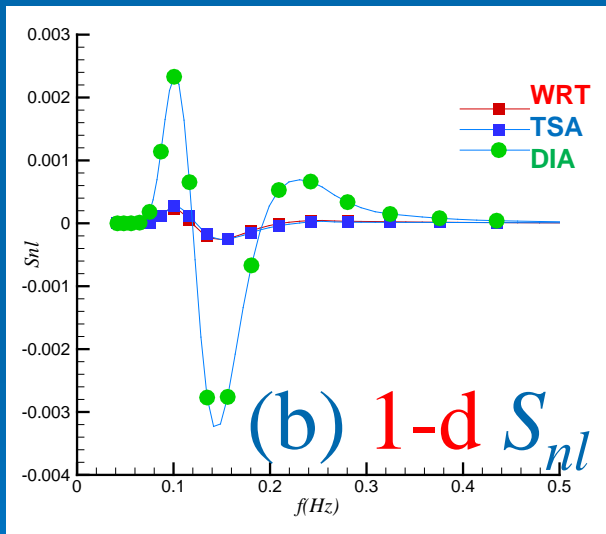
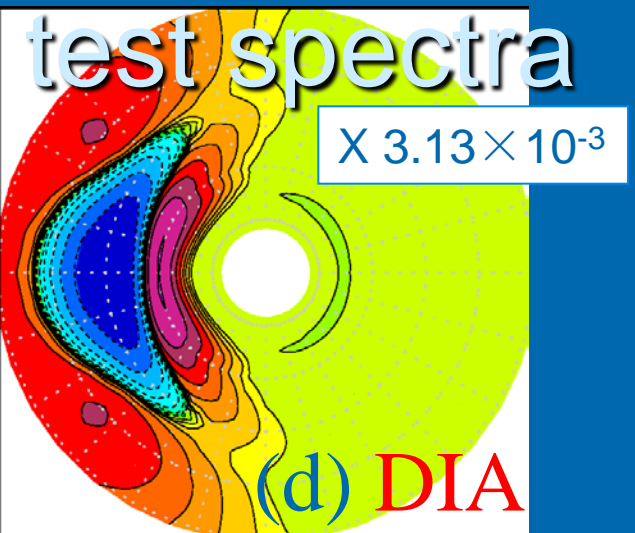
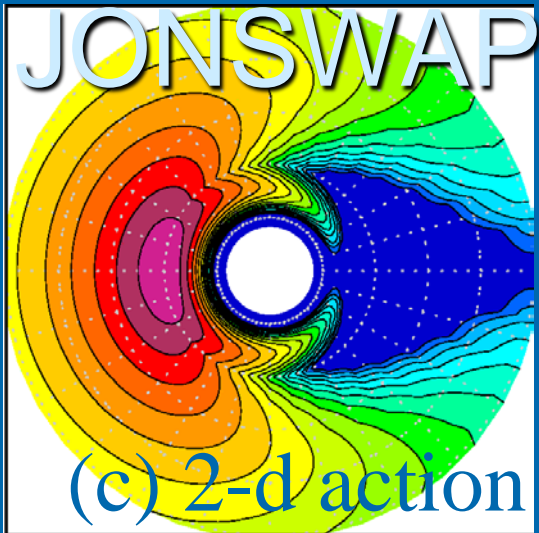
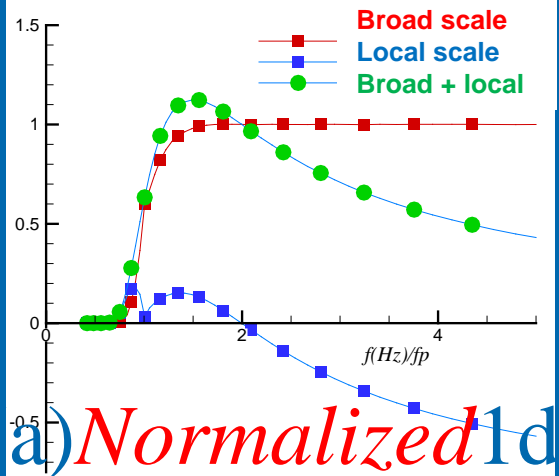
$$T(\mathbf{k}_1, \mathbf{k}_3) = 2 \oint [n_1 n_3 (n_4 - n_2) + n_2 n_4 (n_3 - n_1)] C(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3, \mathbf{k}_4) \theta(|\mathbf{k}_1 - \mathbf{k}_4| - |\mathbf{k}_1 - \mathbf{k}_3|) |\partial W / \partial n|^{-1} ds,$$

TSA – Two-Scale Approximation

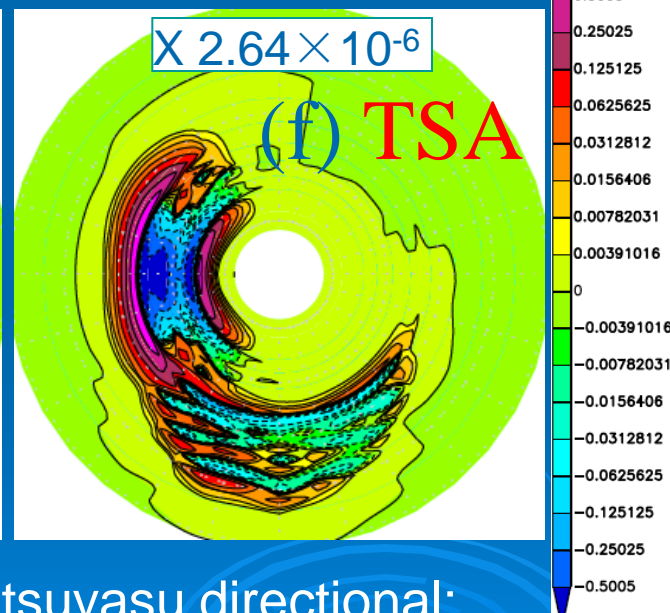
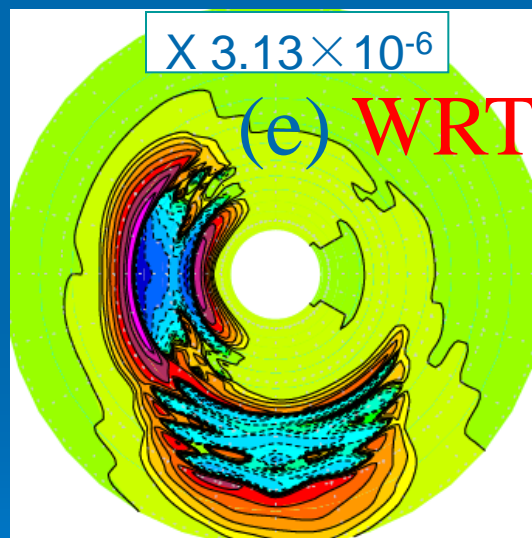
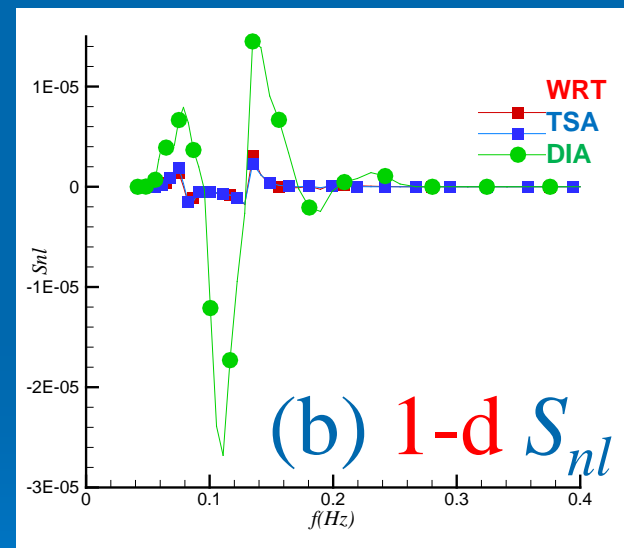
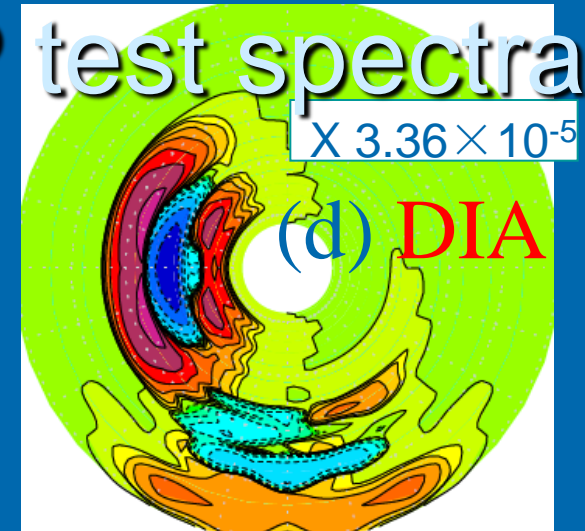
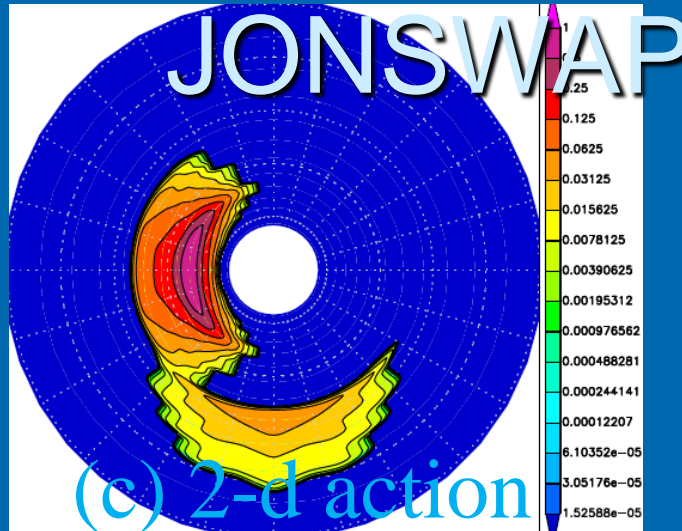
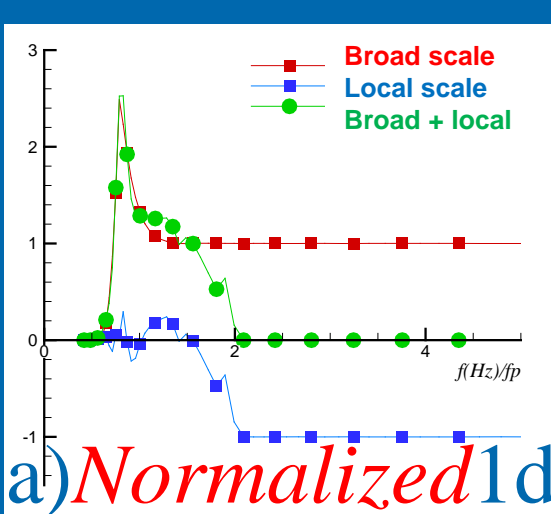
$$n_i = n_i [\text{broad-scale}] + n_i [\text{local-scale}] ; i = 1, 2, 3, 4$$

Neglect n_2 [local-scale] and n_4 [local-scale]

[Resio and Perrie 2008; Perrie & Resio 2009]



JONSWAP $\gamma=1$ with Hasselmann-Mitsuyasu directional:
 (a) broad- and local-scale terms normalized by f^{-4} ,
 (b) 1-d comparison of DIA, WRT and TSA, (c) 2-d action density n_i ,
 (d) $S_{nl}(f, \theta)$ results from DIA (e) WRT, (f) TSA. $f_p=0.1$, $\alpha=0.0081$, $\sigma_A=0.07$, $\sigma_B=0.09$.



JONSWAP sheared spectrum with Hasselmann-Mitsuyasu directional:

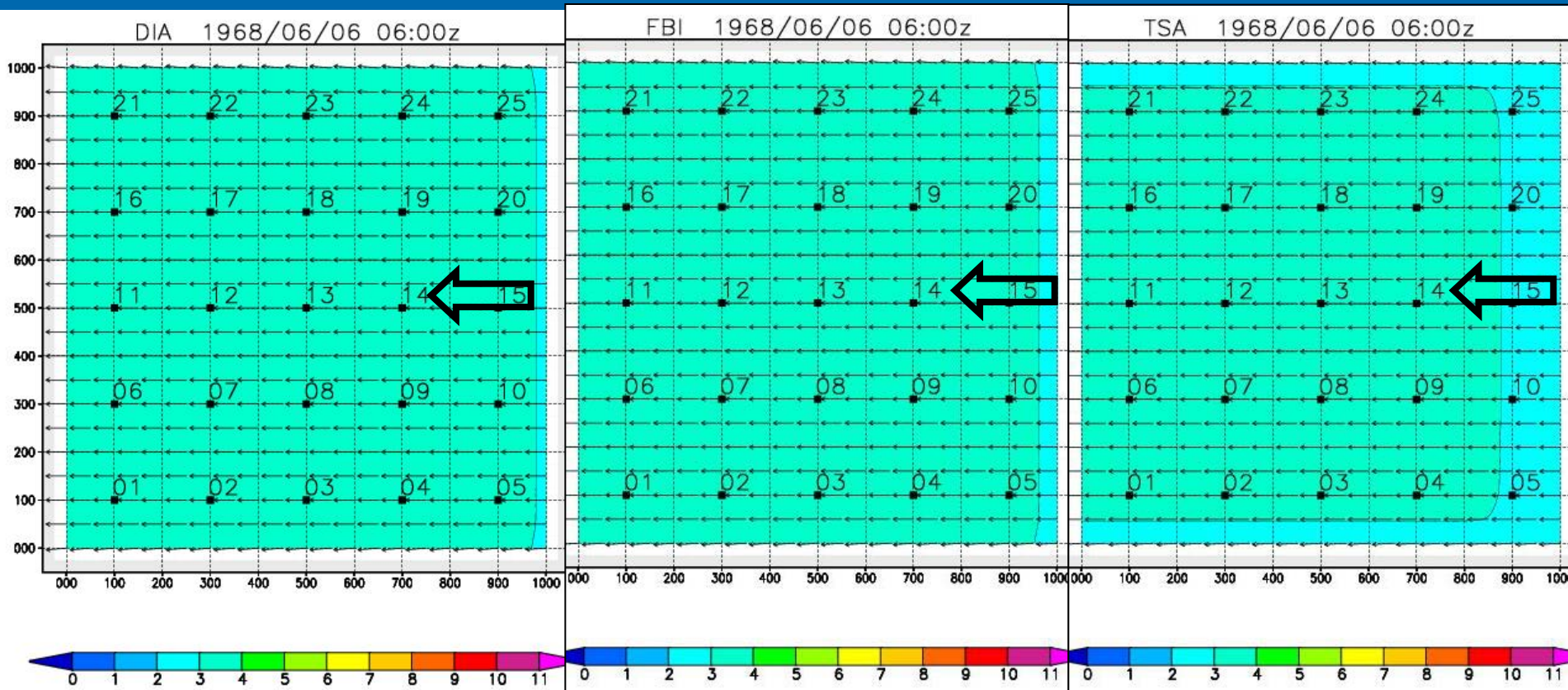
(a) broad- and local-scale terms normalized by f^{-4} ,

(b) 1-d comparison of DIA, WRT and TSA, (c) 2-d action density n_i ,

(d) $S_{nl}(f, \theta)$ results from DIA (e) WRT (f) TSA. $f_p=0.1$, $\alpha=0.0081$, $\sigma_A=0.07$, $\sigma_B=0.09$.

WW3 – with 'old' ST1: fetch-limited growth

6 hr



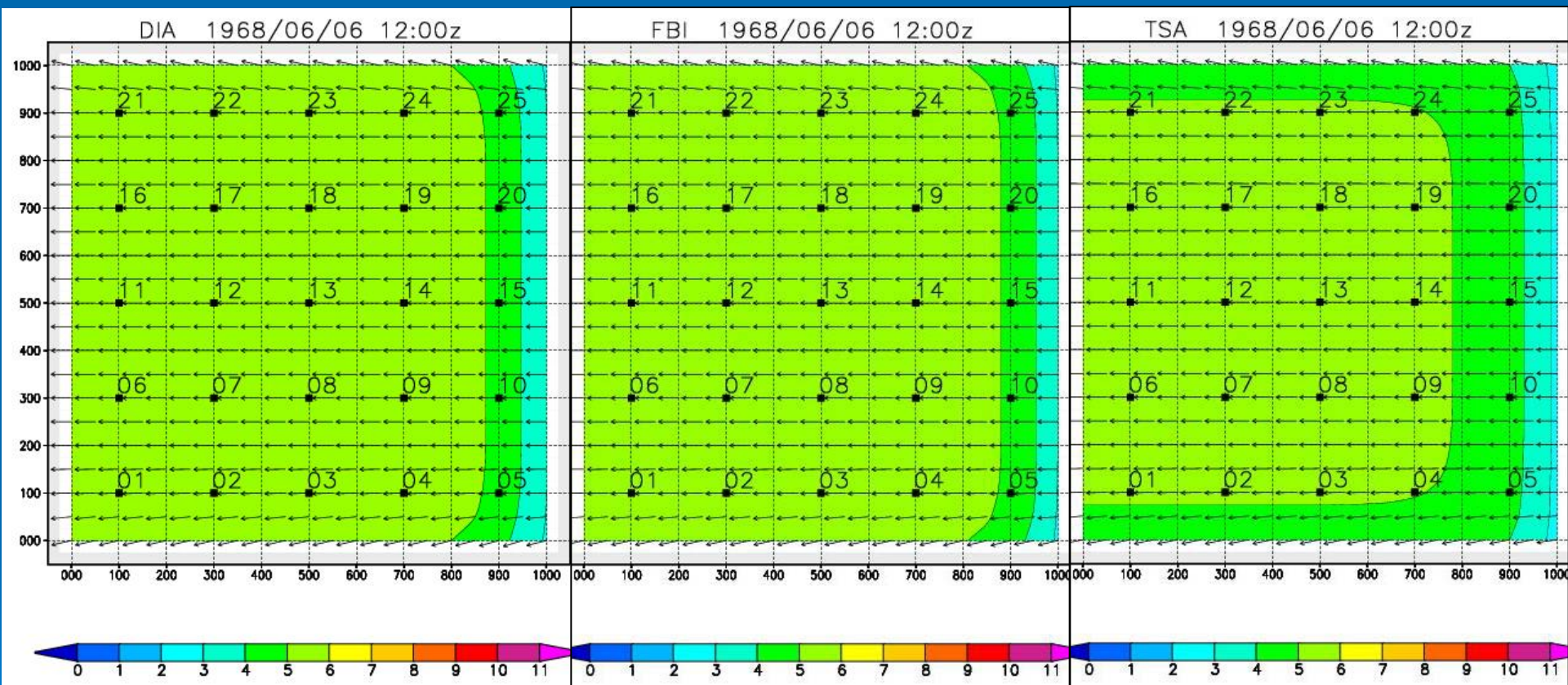
DIA

FBI

TSA

WW3 – with 'old' ST1: fetch-limited growth

12 hr



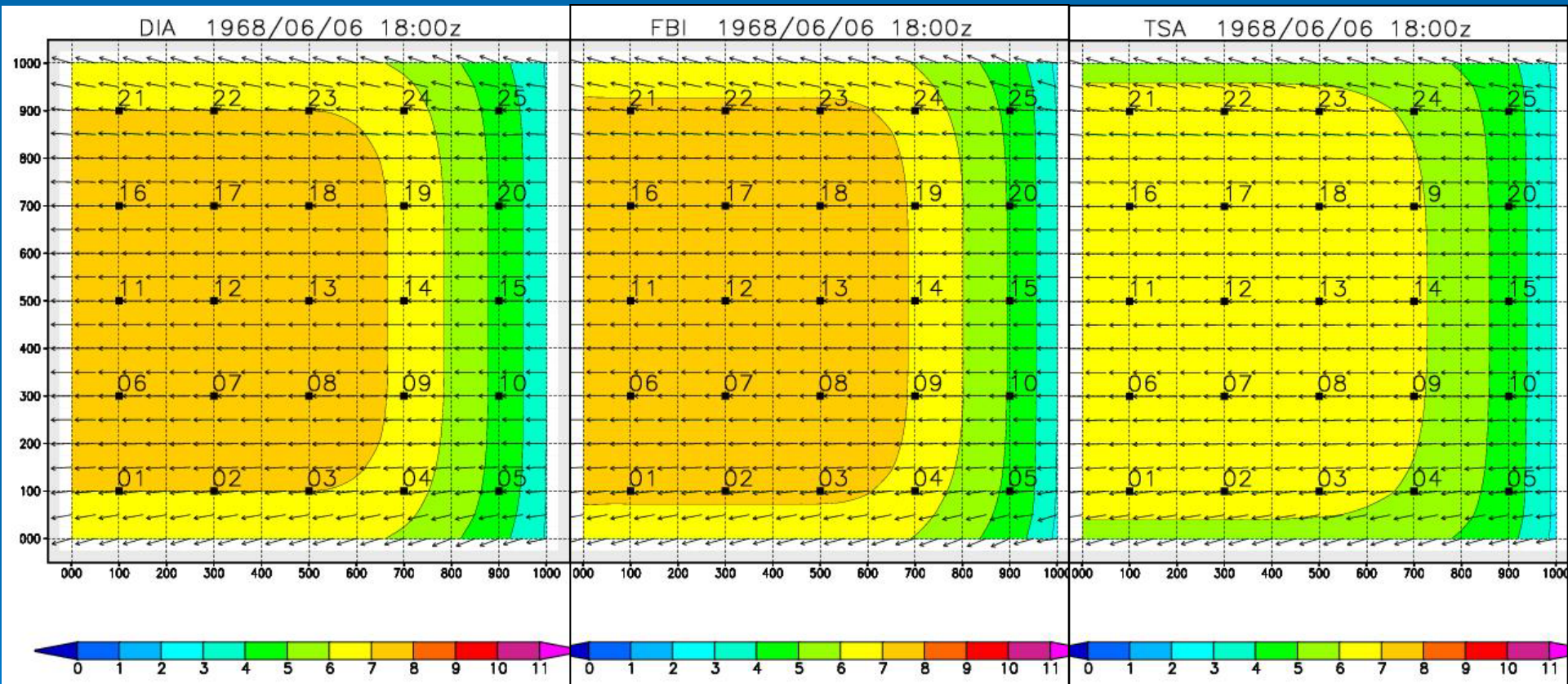
DIA

FBI

TSA

WW3 – with 'old' ST1: fetch-limited growth

18 hr



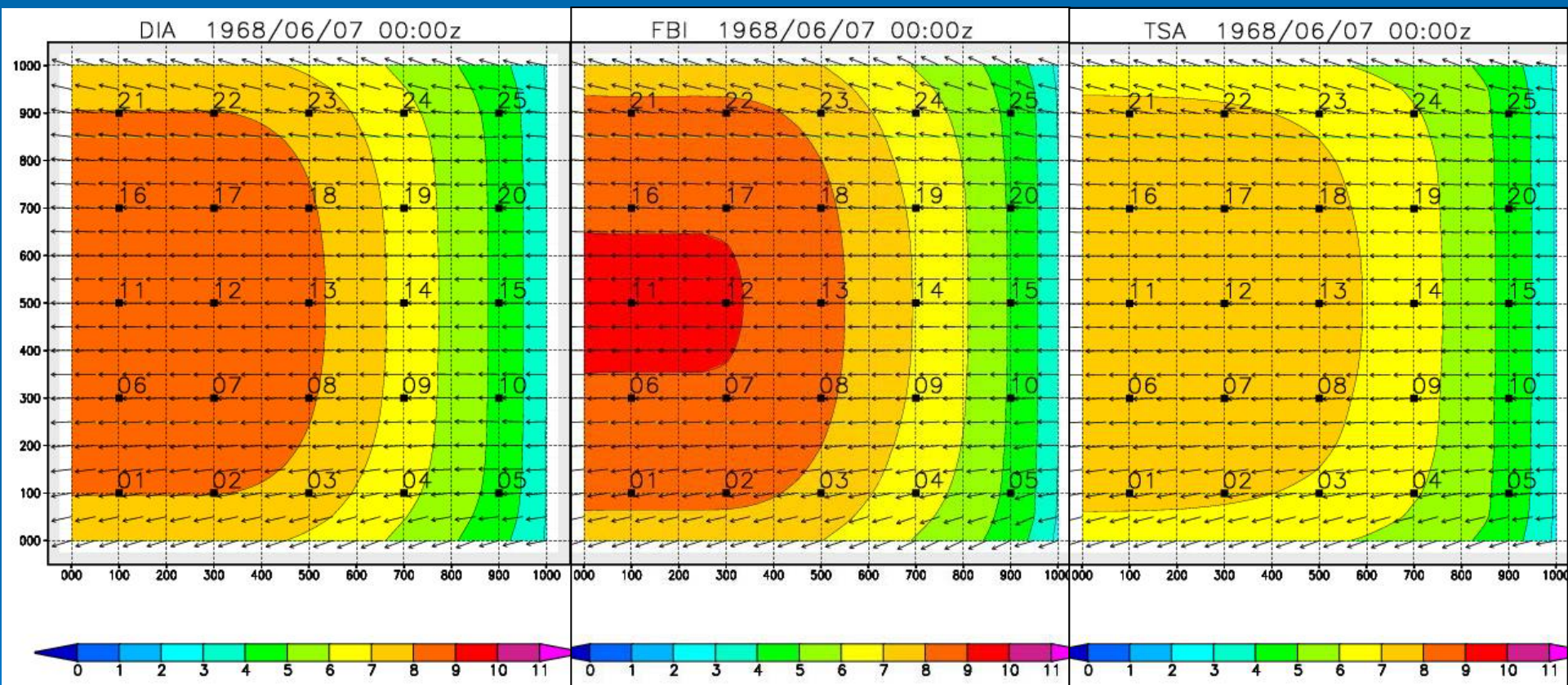
DIA

FBI

TSA

WW3 – with 'old' ST1: fetch-limited growth

24 hr



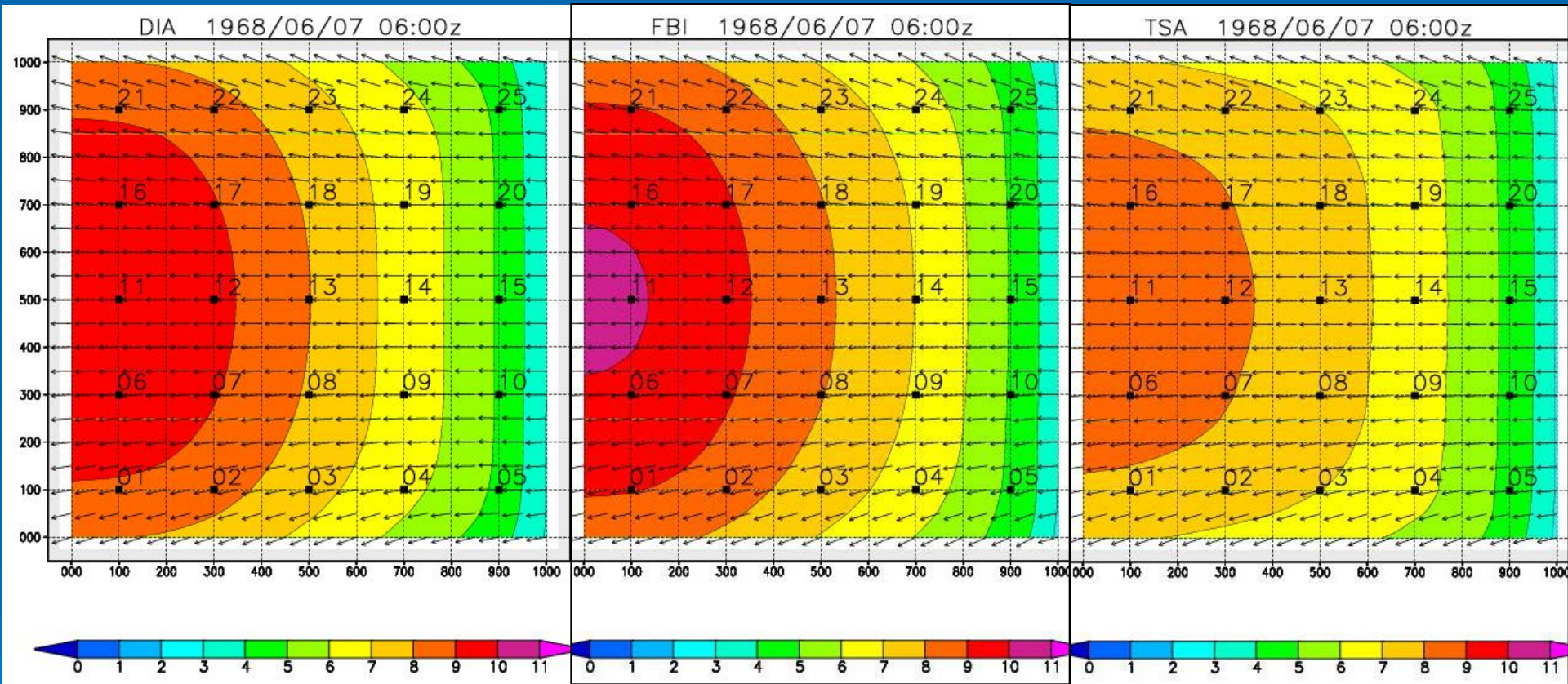
DIA

FBI

TSA

WW3 – with ‘old’ ST1: fetch-limited growth

30 hr



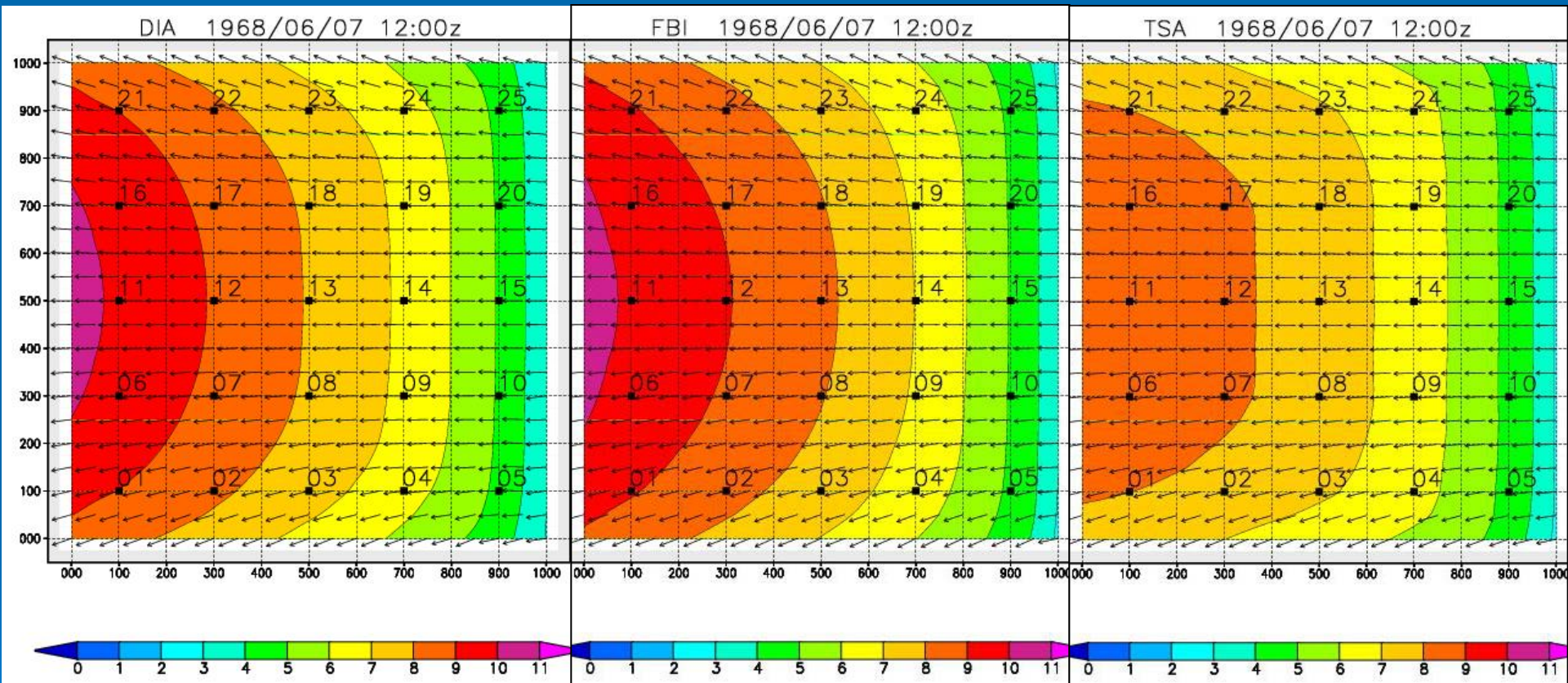
DIA

FBI

TSA

WW3 – with ‘old’ ST1: fetch-limited growth

36 hr



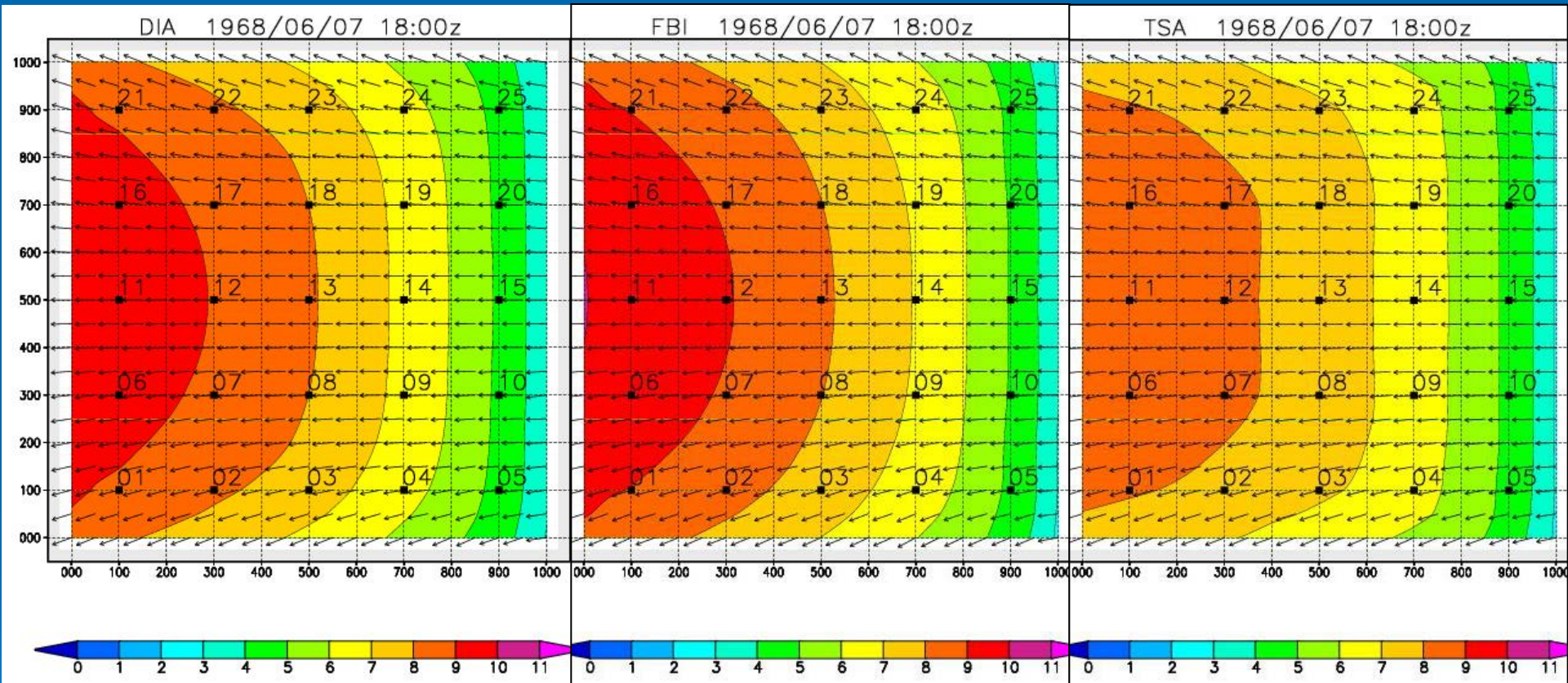
DIA

FBI

TSA

WW3 – with 'old' ST1: fetch-limited growth

42 hr

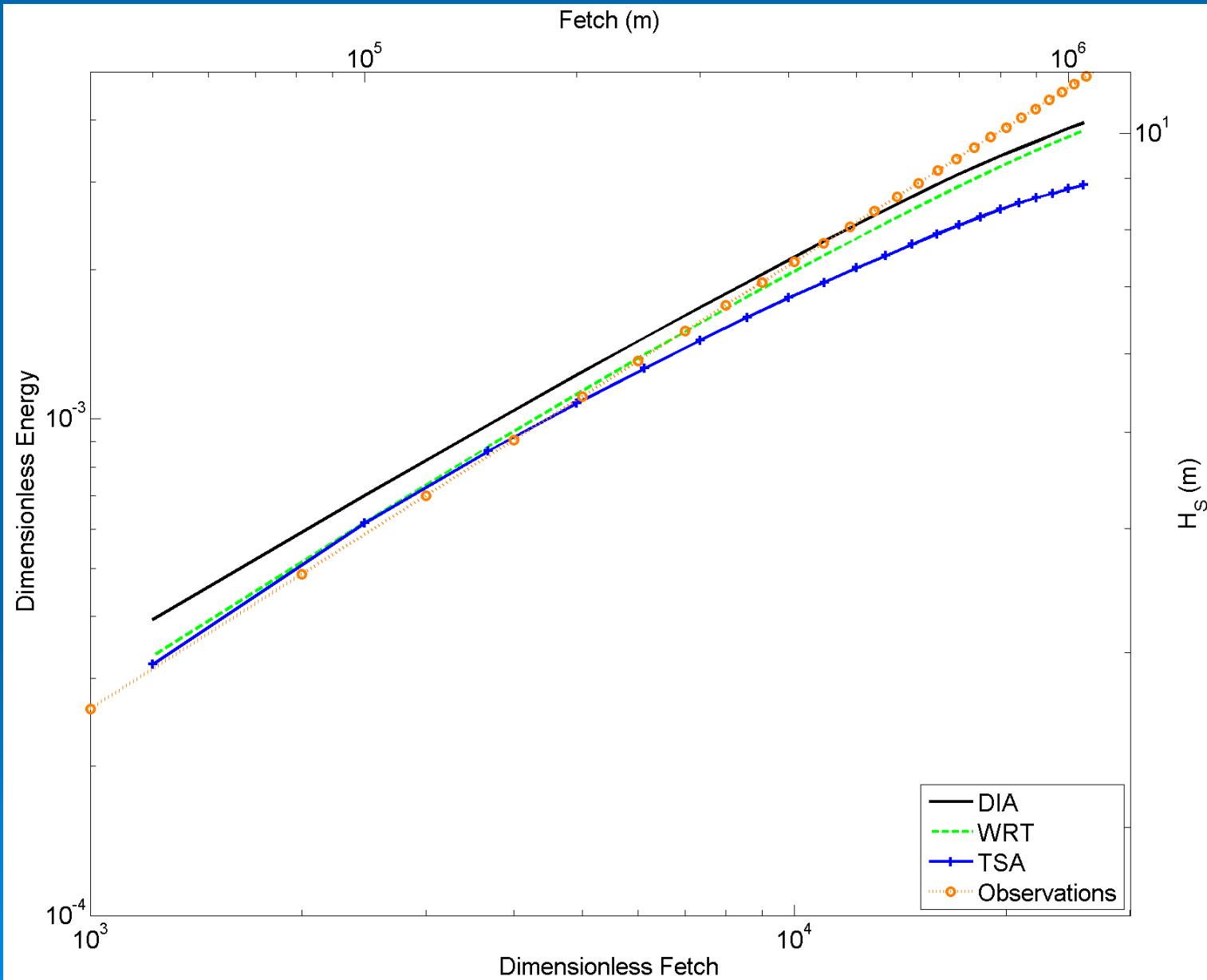


DIA

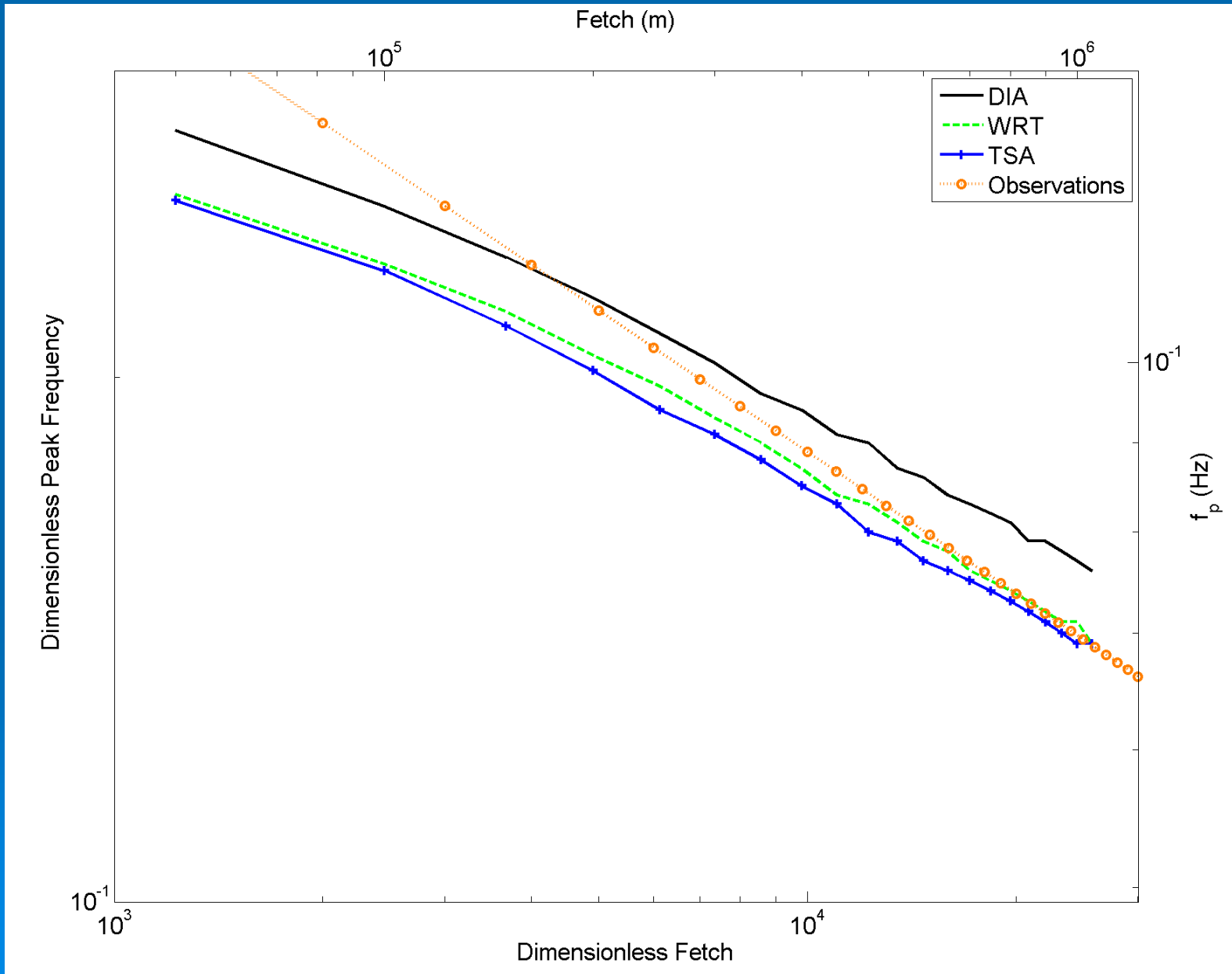
FBI

TSA

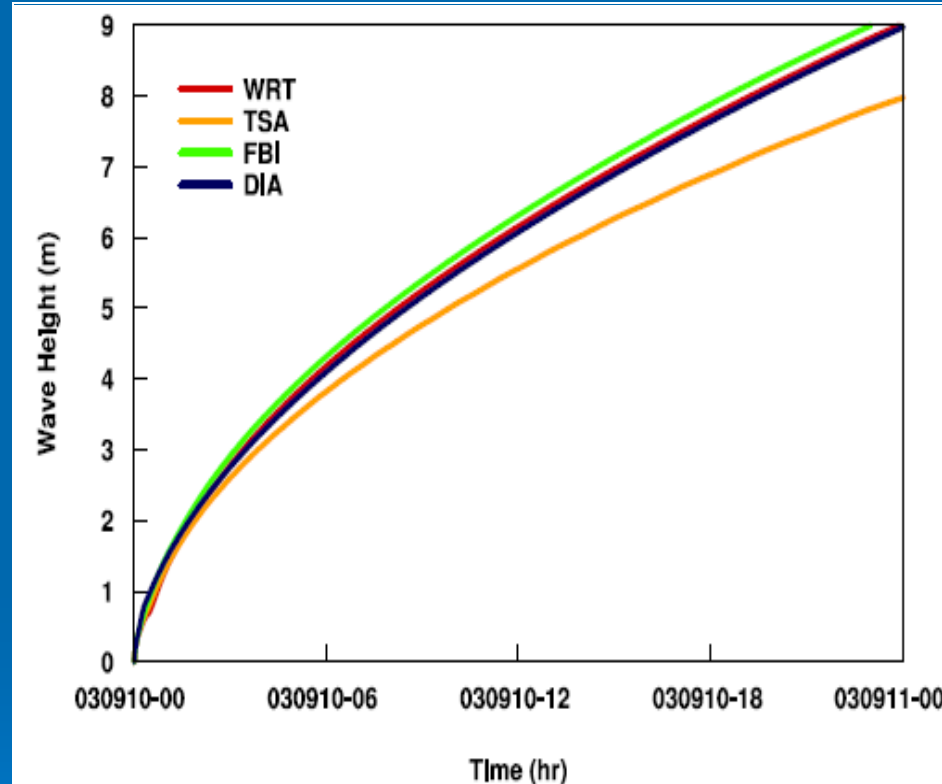
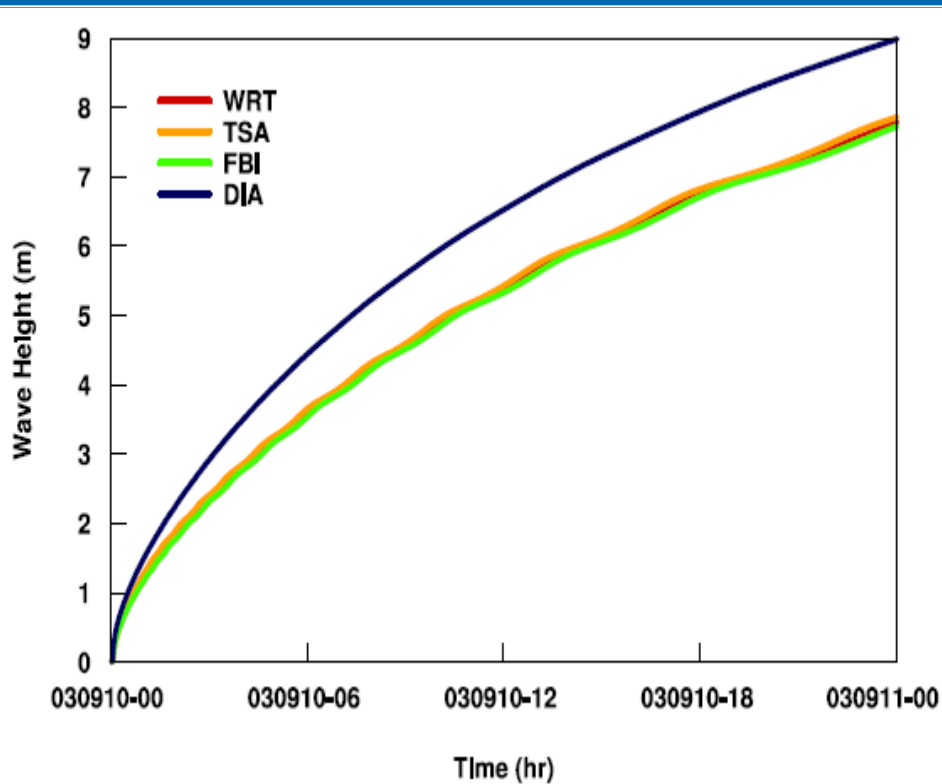
WW3 – with 'old' ST1: fetch-limited growth



WW3 – with ‘old’ ST1: fetch-limited growth



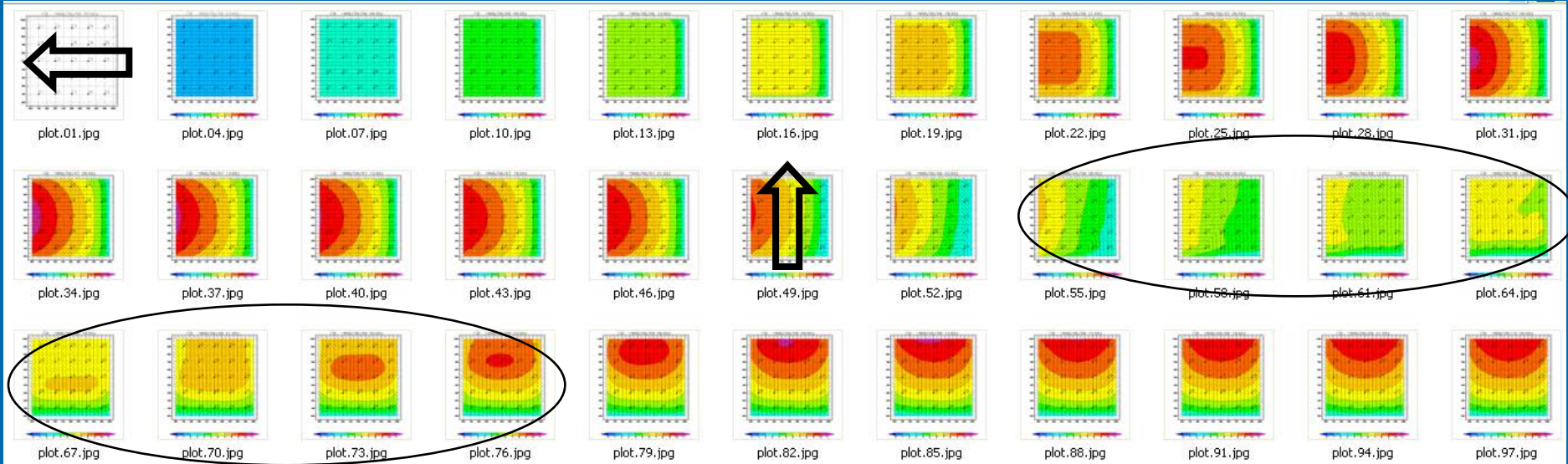
1-point time integration



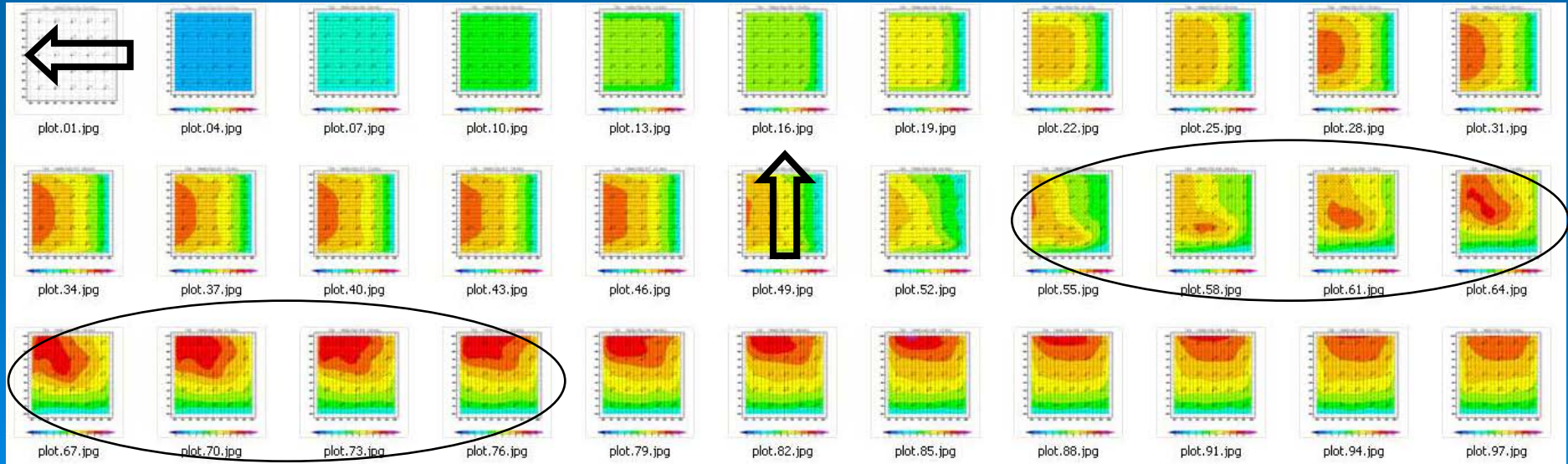
WWM (Roland et al., 2012) with **ST4**
From Ardhuin et al. (2010)

WW3 (Tolman, 2009) with **ST2**
From Tolman + Chalikov (1996)

Ongoing issue: turning winds by 90° at 48 hr

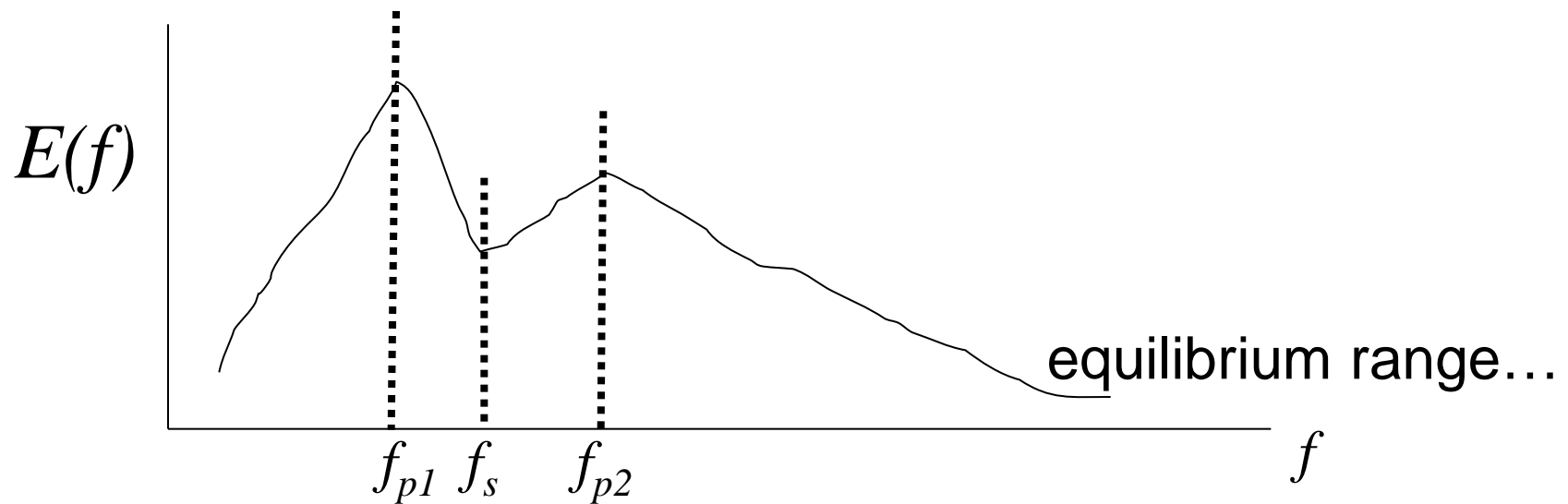


WRT with ST1



original TSA with ST1

Multiple spectral peaks - mTSA



Broad-scale term parameterization...?

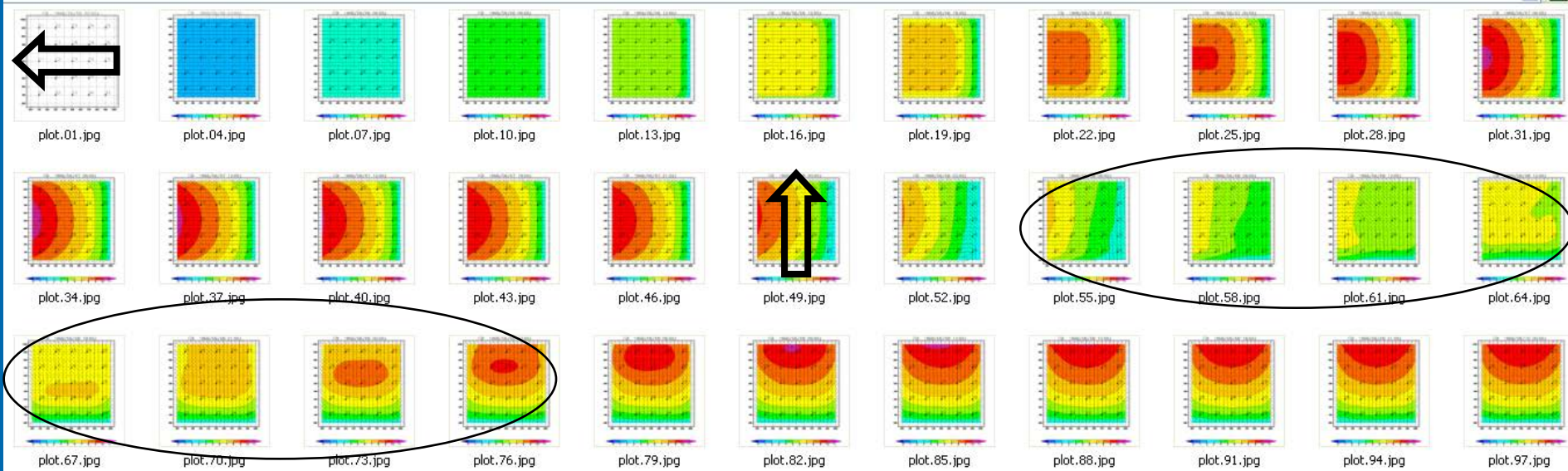
$$F(k)_{Norm} = F(k) \times k^{2.5} / \beta \quad [\text{Resio\&Perrie, 1989; Resio et al. 2004...}]$$

Should be $\beta \sim 1/\Delta f \sum [F(k) \times k^{2.5}]_{\text{equilibrium range}}$

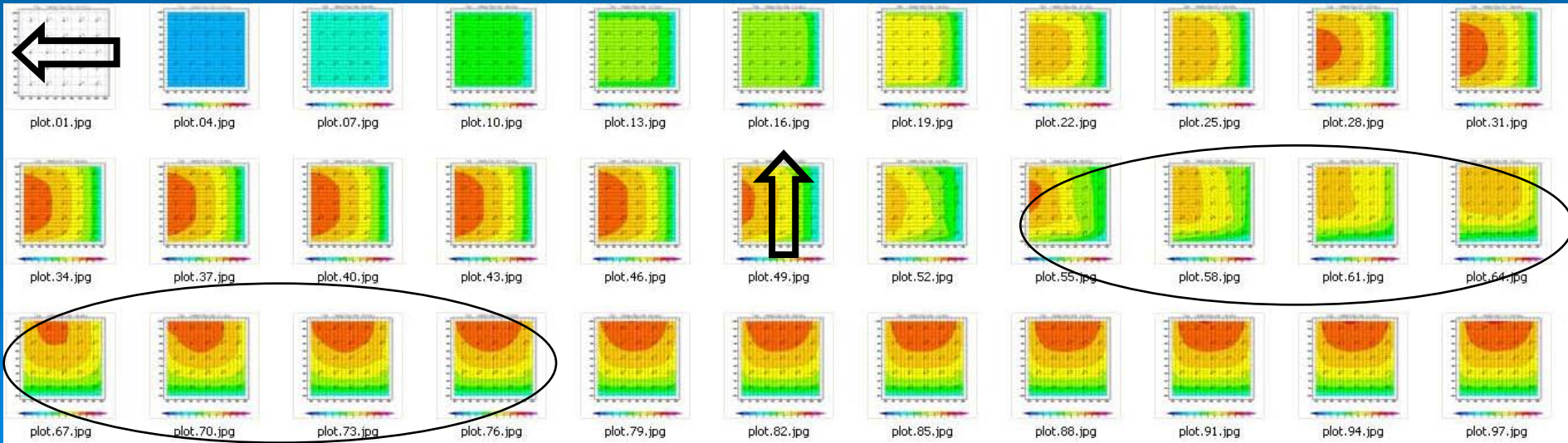
But equilibrium range is hard to define when f_{p1} and f_{p2} are close...

So let $\beta = F(k) \times k^{2.5} / f_s \dots$ *for the first peak ...*

Ongoing issue: turning winds by 90° at 48 hr

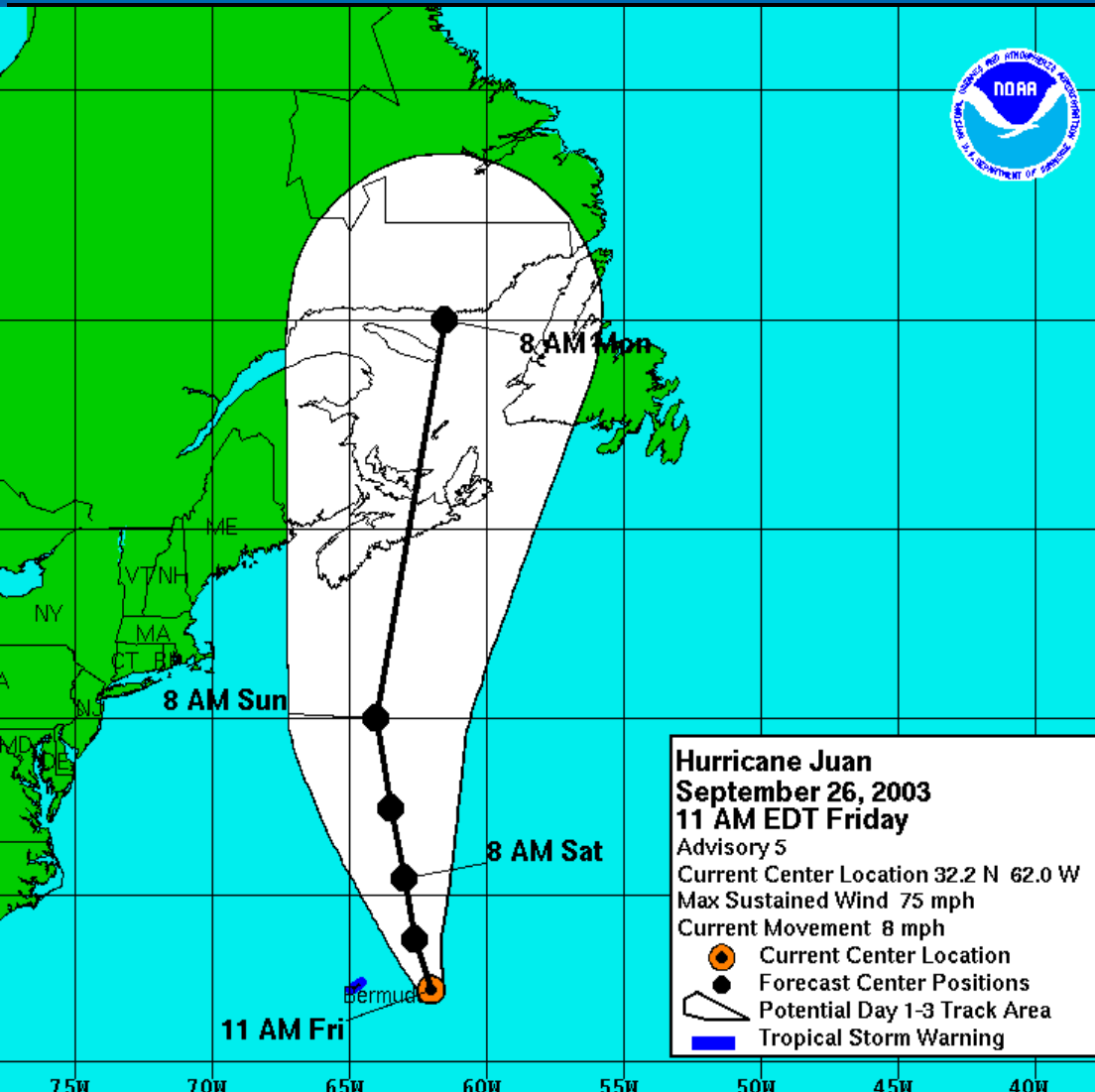


WRT with ST1



New double-peak dTSA with ST1

Hurricane Juan (2003)

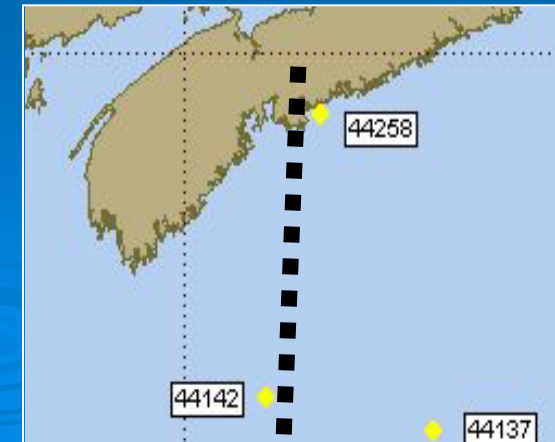


Track at max. wind radius

2-3 AM UTC 29 Sept.

MSL

k



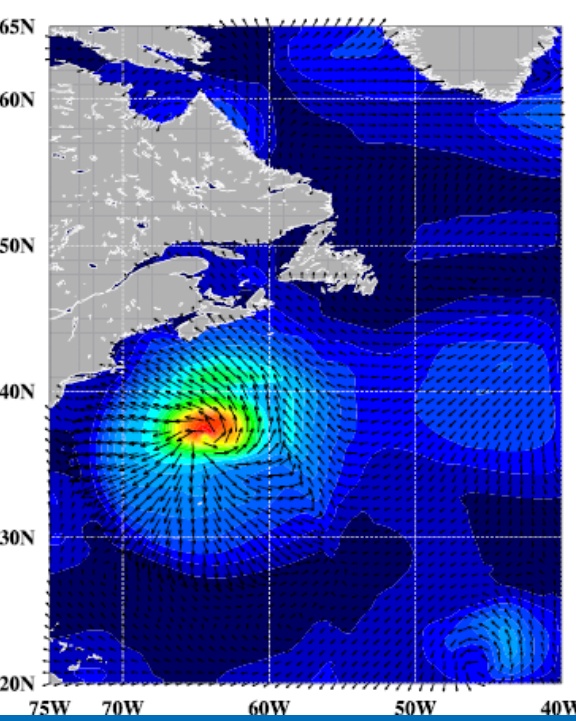
Hurricane Juan wave heights, H_s

DIA

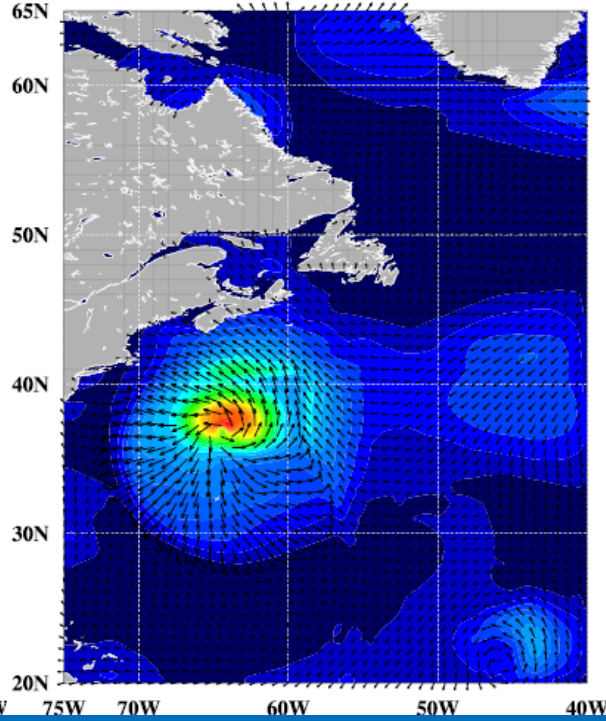
FBI

difference DIA-FBI

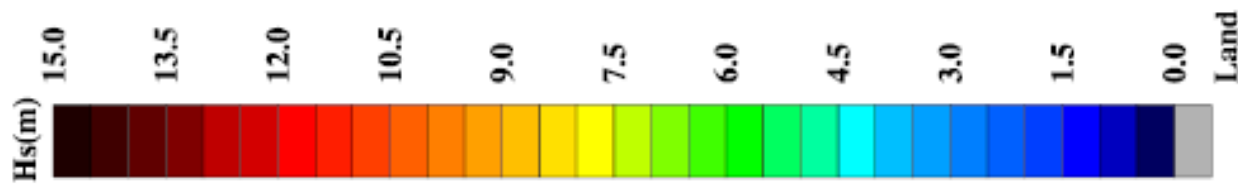
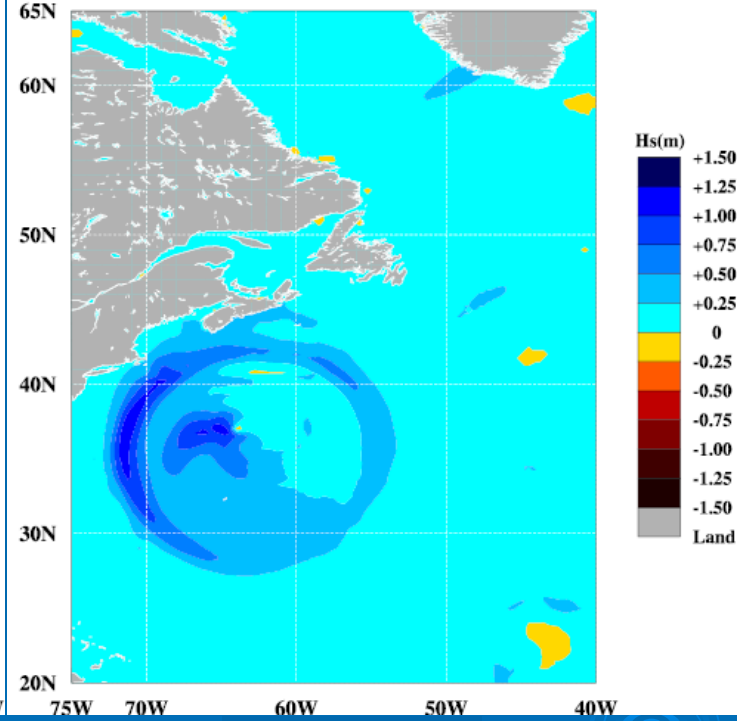
DIA: Sig. Wave Heights at 20030928 05



WRT: Sig. Wave Heights at 20030928 05



DIA - WRT: Sig. Wave Heights at 20030928 05



~10%

Hurricane Juan wave heights, H_s

DIA

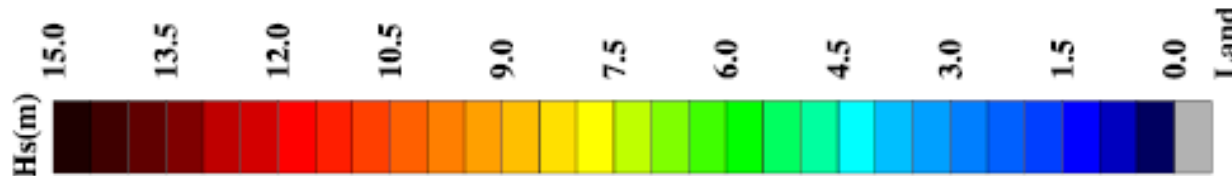
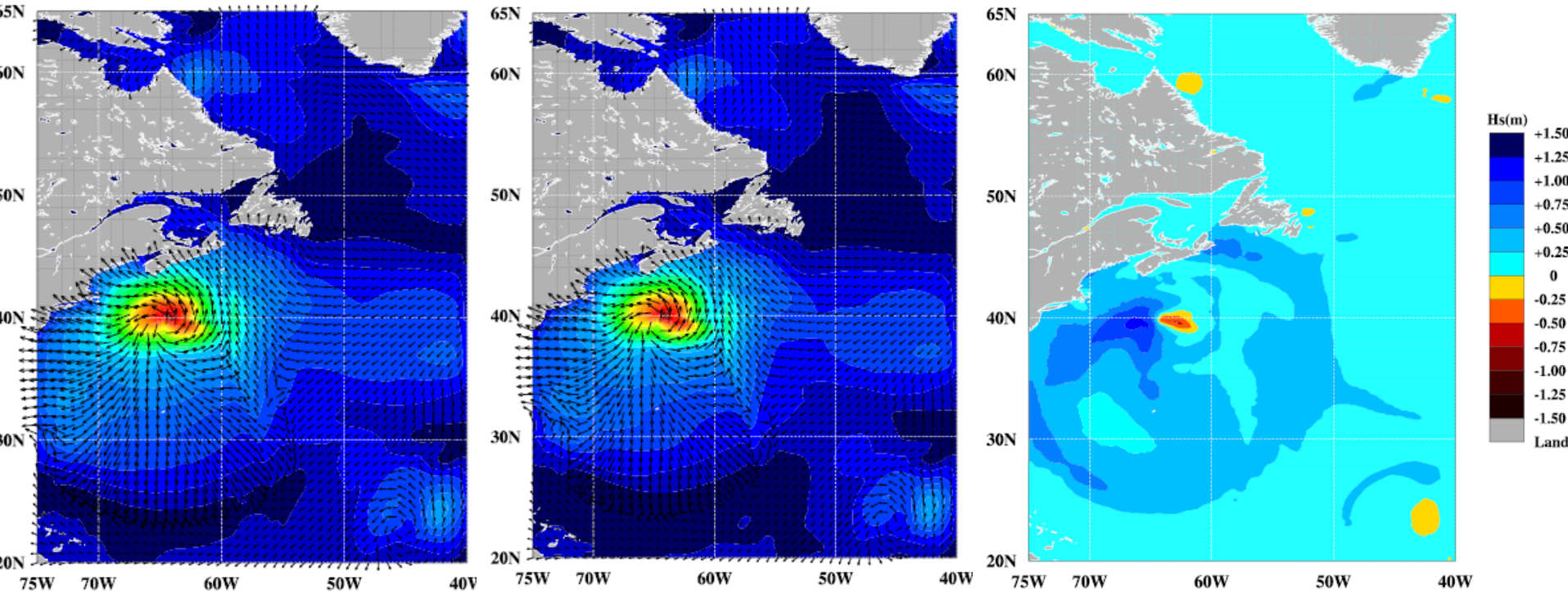
FBI

difference DIA-FBI

DIA: Sig. Wave Heights at 20030928 17

WRT: Sig. Wave Heights at 20030928 17

DIA - WRT: Sig. Wave Heights at 20030928 17



~15%

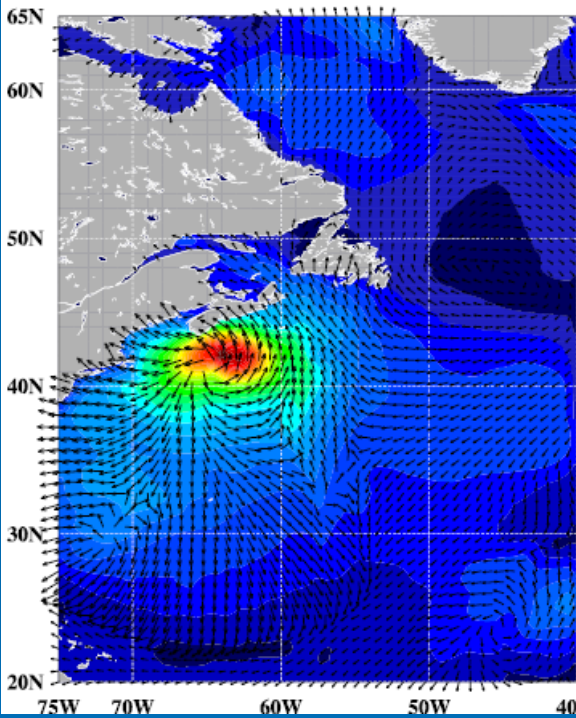
Hurricane Juan wave heights, H_s

DIA

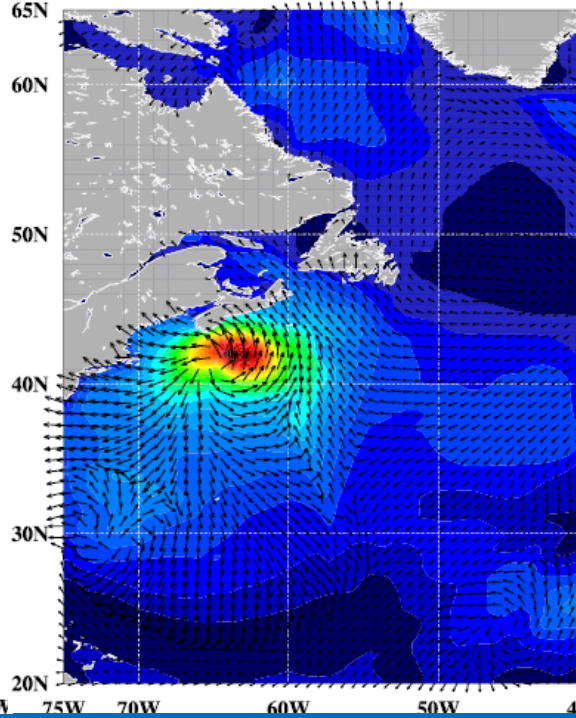
FBI

difference DIA-FBI

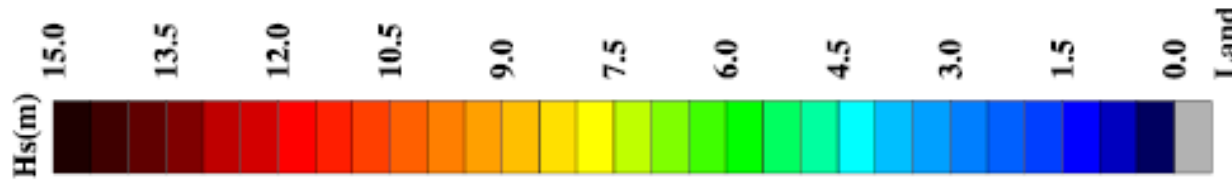
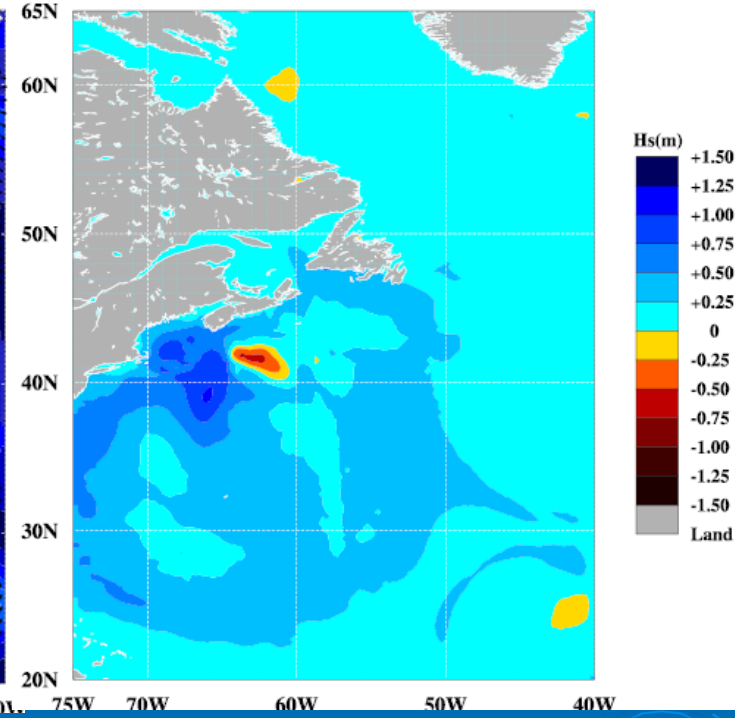
DIA: Sig. Wave Heights at 20030928 23



WRT: Sig. Wave Heights at 20030928 23



DIA - WRT: Sig. Wave Heights at 20030928 23



~15%

Hurricane Juan wave heights, H_s

DIA

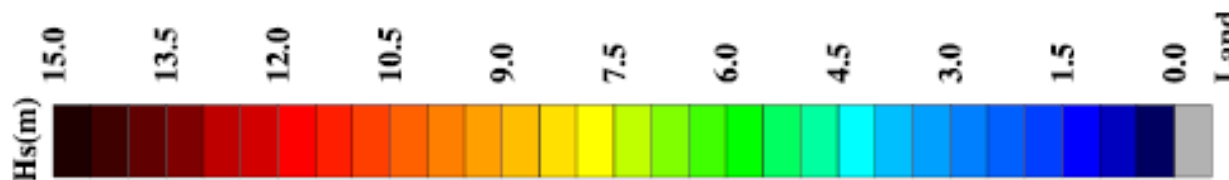
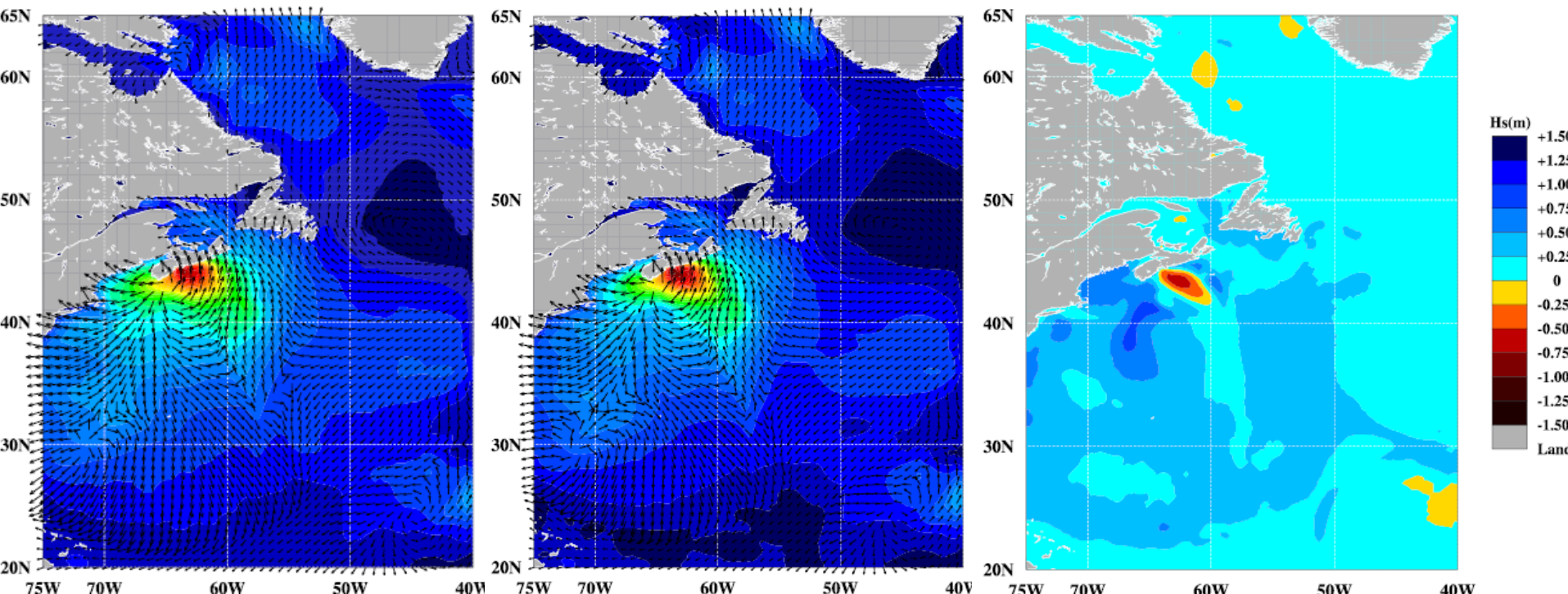
FBI

difference DIA-FBI

DIA: Sig. Wave Heights at 20030929 03

WRT: Sig. Wave Heights at 20030929 03

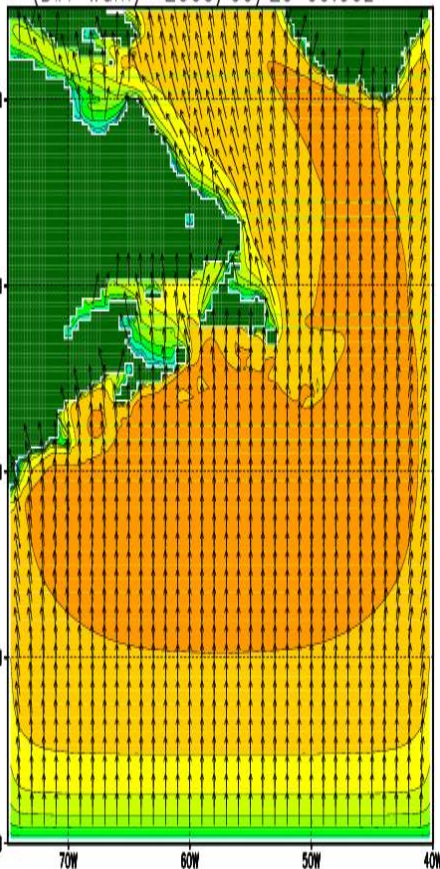
DIA - WRT: Sig. Wave Heights at 20030929 03



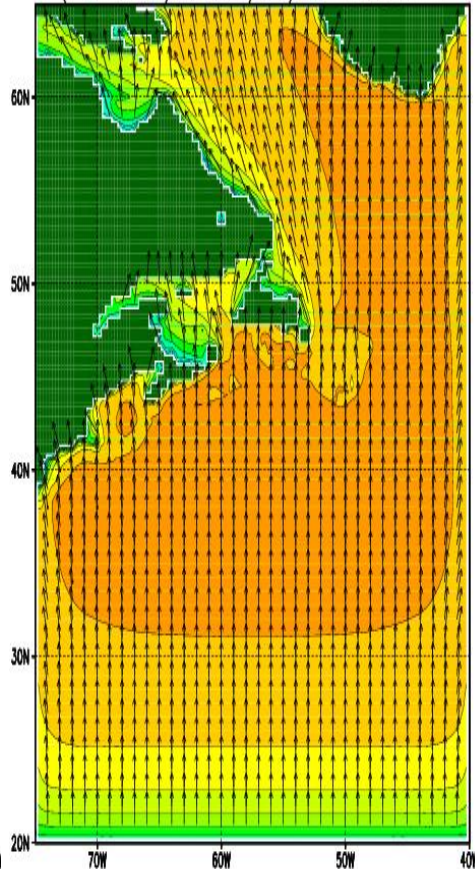
~15%

WW3 – constant U10 – 55 hr ‘old’ **ST1**

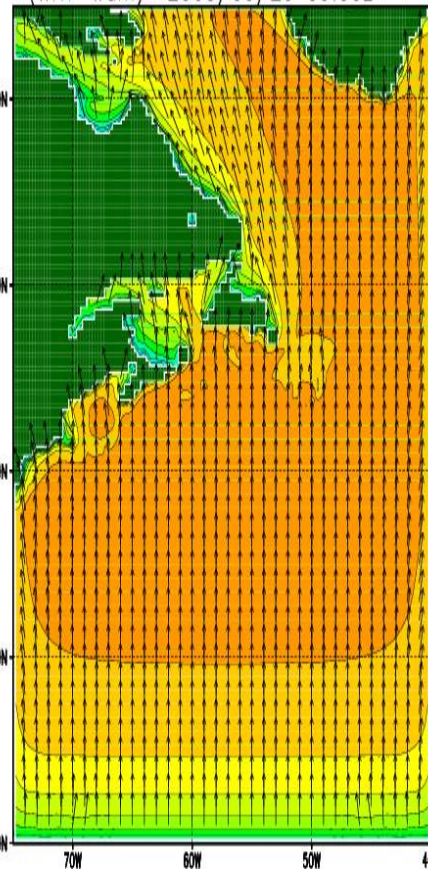
(DIA-wam) 2003/09/29 09:00z



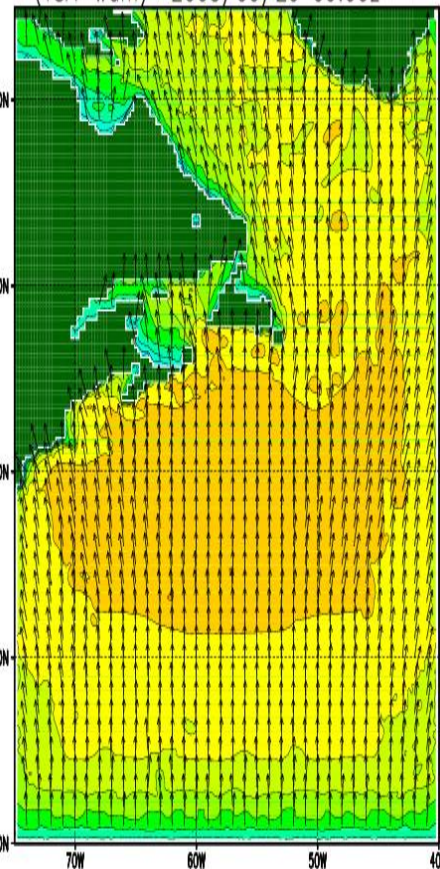
(FBI-wam) 2003/09/29 09:00z



(WRT-wam) 2003/09/29 09:00z

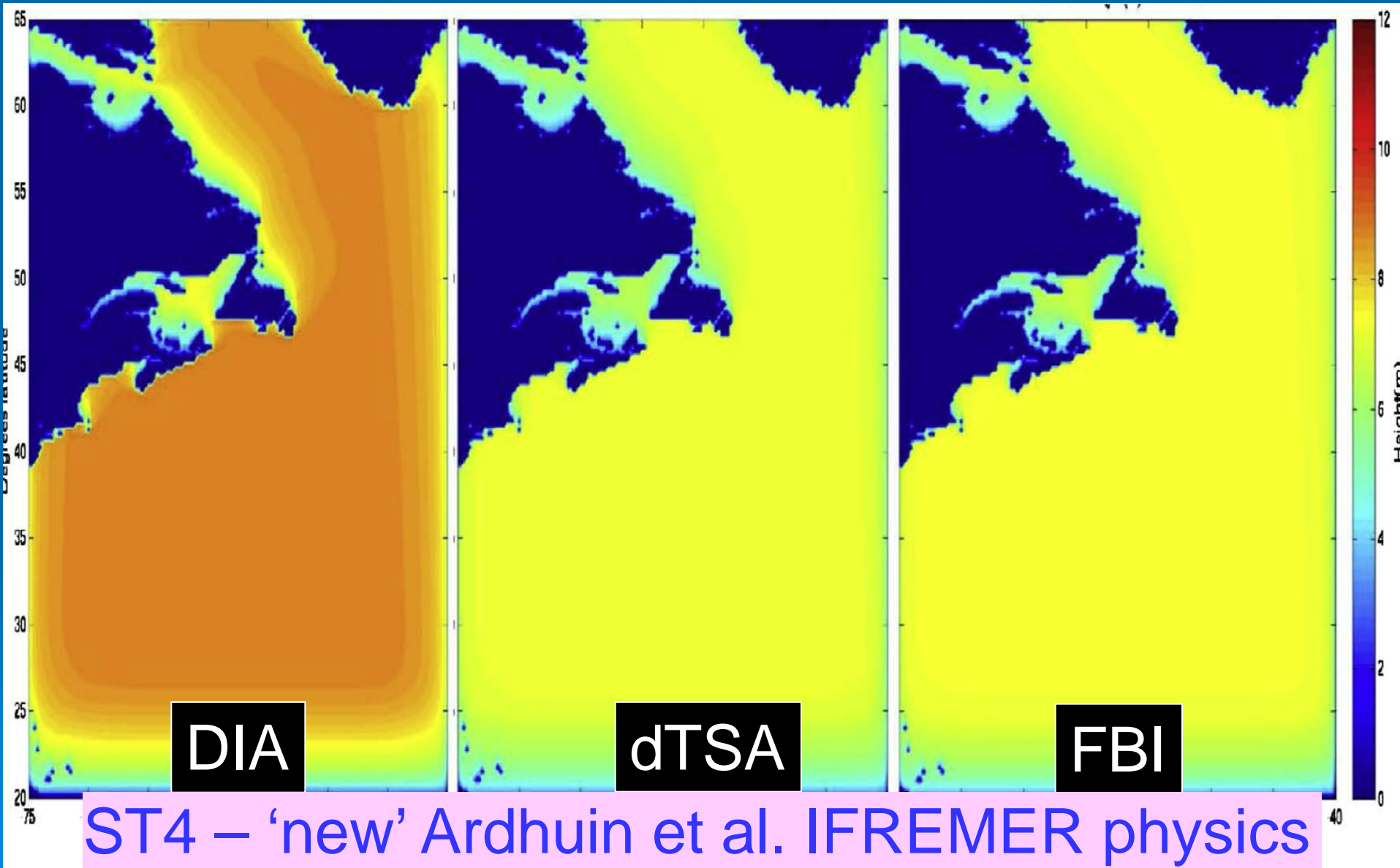


(TSA-wam) 2003/09/29 09:00z



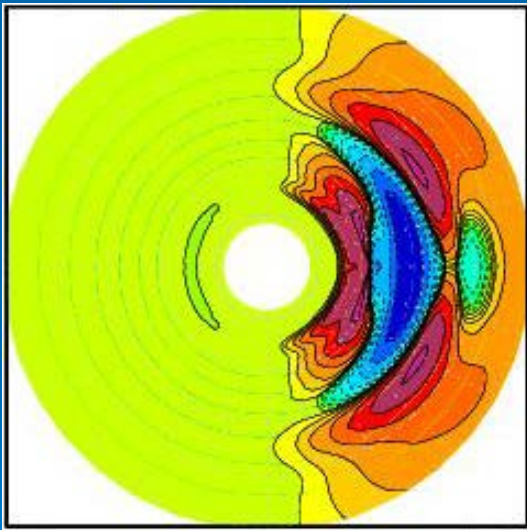
ST1 – wamCy3 physics

WW3 – constant U10 – 55 hr ‘new’ **ST4**

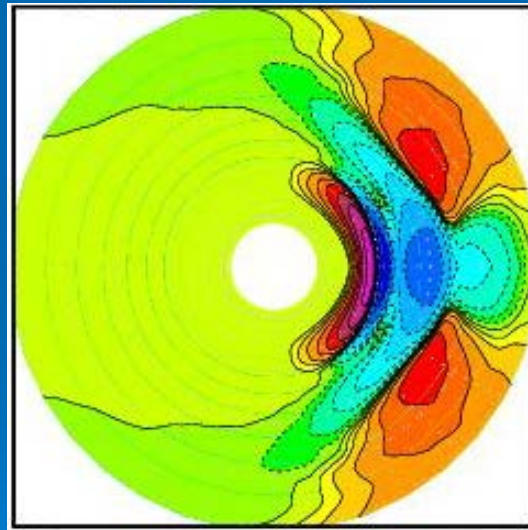


Computational time

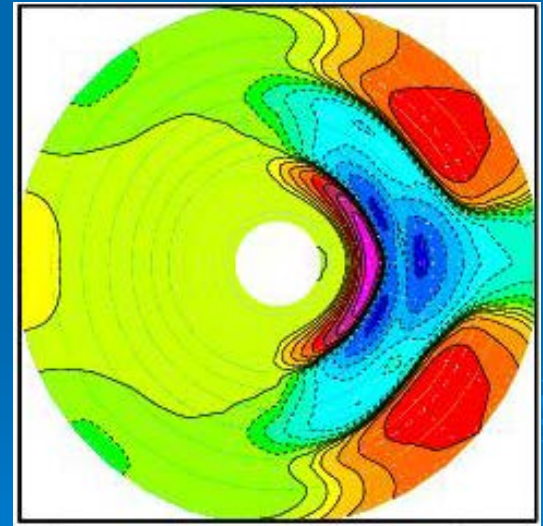
- Alternate frequency, angles & interaction points can speed up TSA about 30-40 × or more
- Presently, best accurate results are 20 × DIA
- Optimization of TSA code is ongoing



DIA



WRT



dTSA,a

Summary

1. Implemented TSA in WW3 and WWM
2. Tests with different source terms: ST1 ~ ST4
3. Reliable results for 'academic' JONSWAP tests
4. " " fetch- and duration-limited growth
5. Turning winds: ongoing test ...
6. N Atlantic tests with hypothetical constant winds
7. Computational efficiency improved
8. Optimization of TSA code is ongoing.

Acknowledgements: Panel on Energy R & D, NOPP ONR.