

# An extreme value model for maximum wave heights based on weather types



**A. Rueda, P. Camus, F. Méndez, A. Tomás, A. Luceño**

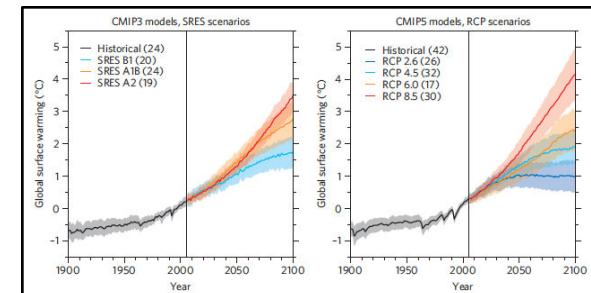
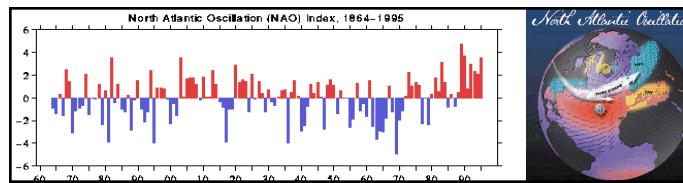
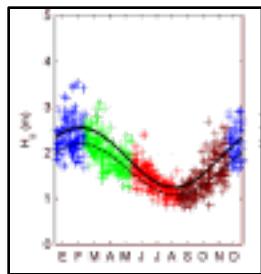
# Motivation

- Interest on the upper tail of the distribution of HS → Extreme value theory

$$F(y) = \exp \left\{ - \left[ 1 + \xi \left( \frac{y-\mu}{\psi} \right) \right]^{-\frac{1}{\xi}} \right\}$$



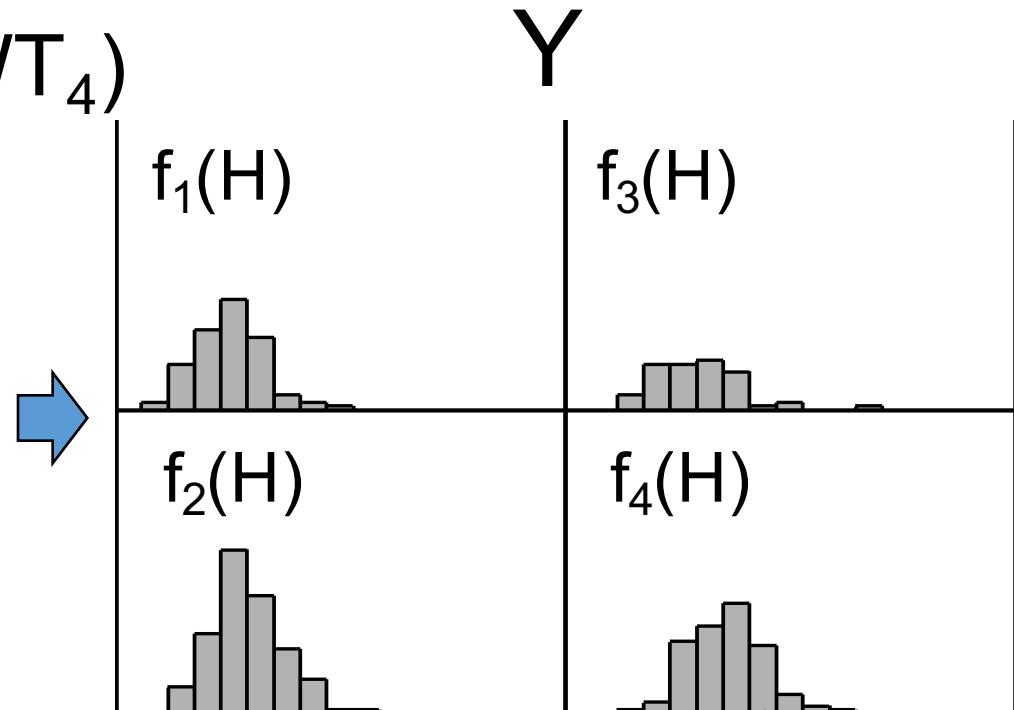
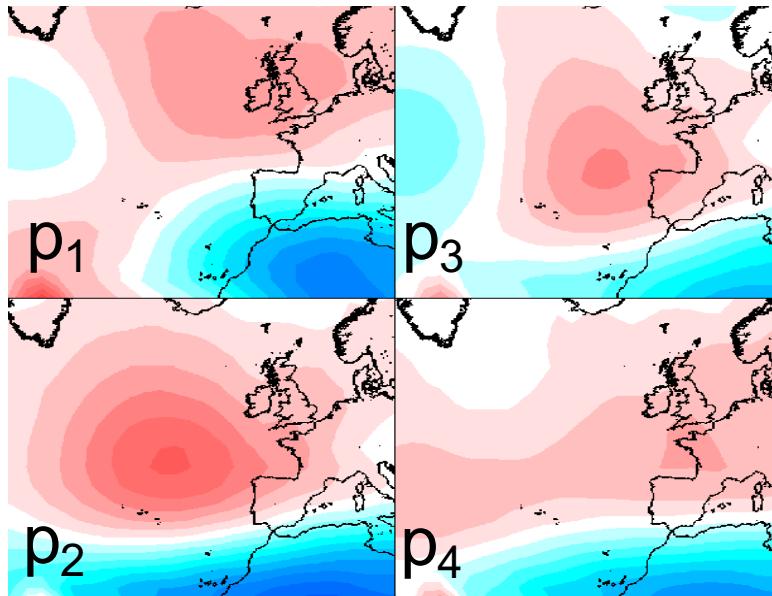
- Non-stationarity of the climate system



- Statistical downscaling of extremes

## SD based on Weather Types

$$X = (WT_1, WT_2, WT_3, WT_4)$$

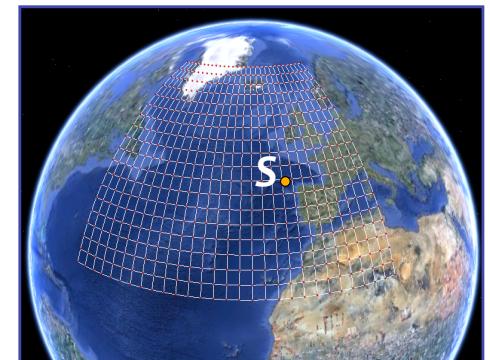


WT= Weather-type

p<sub>i</sub>=occurrence probability of WT<sub>i</sub>

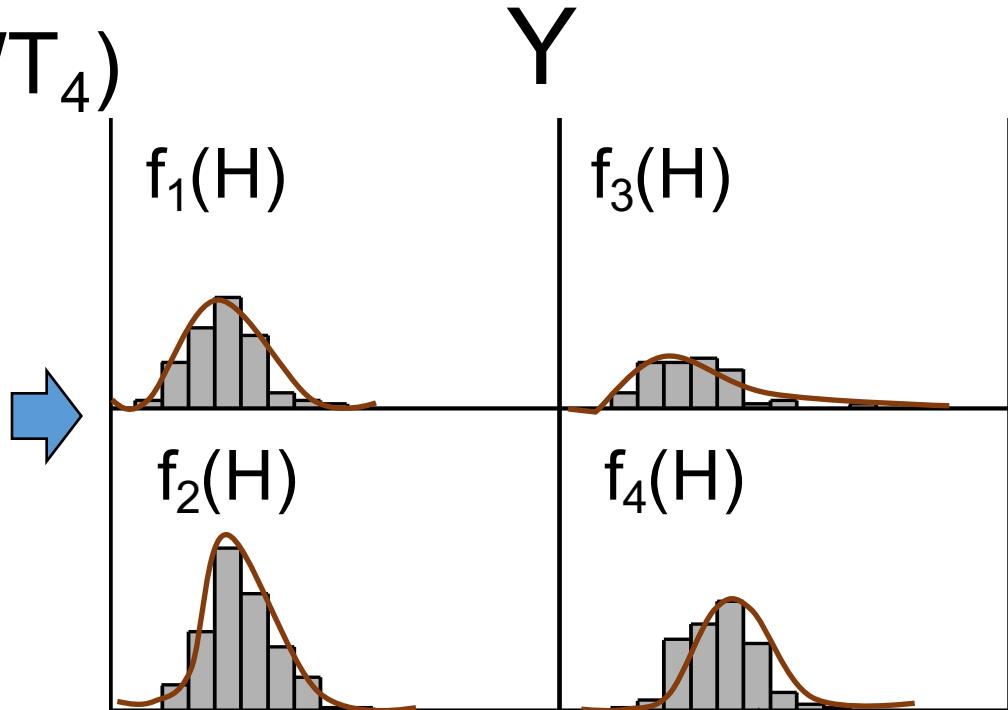
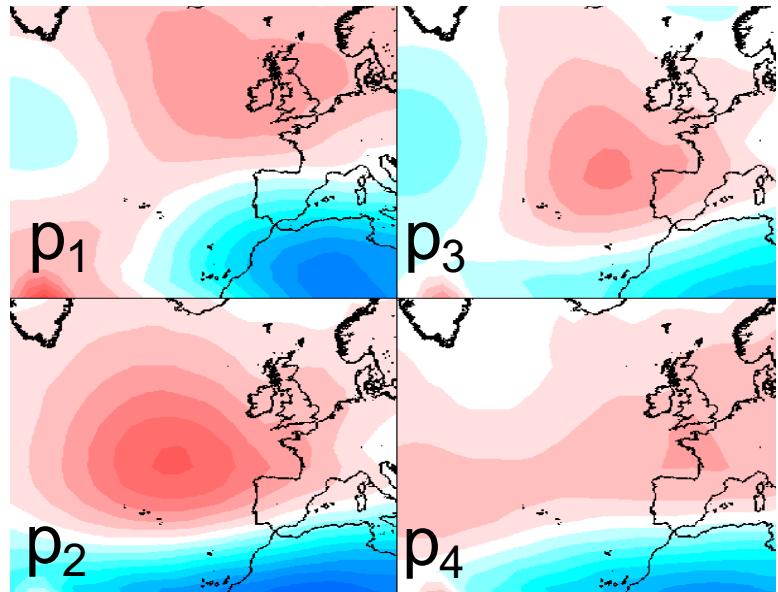
Regression model /Stat. Downscaling:

$$Y = g(X)$$



# Daily max - SD based on Weather Types

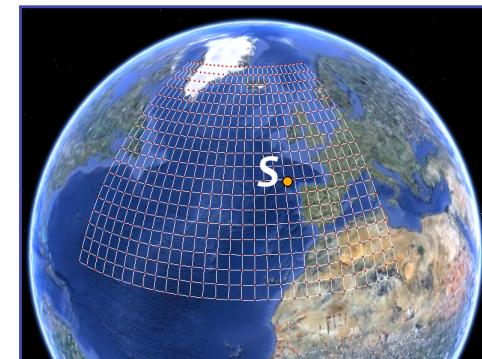
$$X = (WT_1, WT_2, WT_3, WT_4)$$



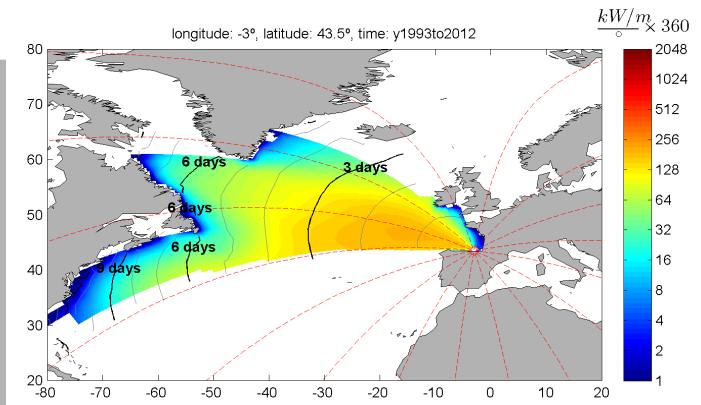
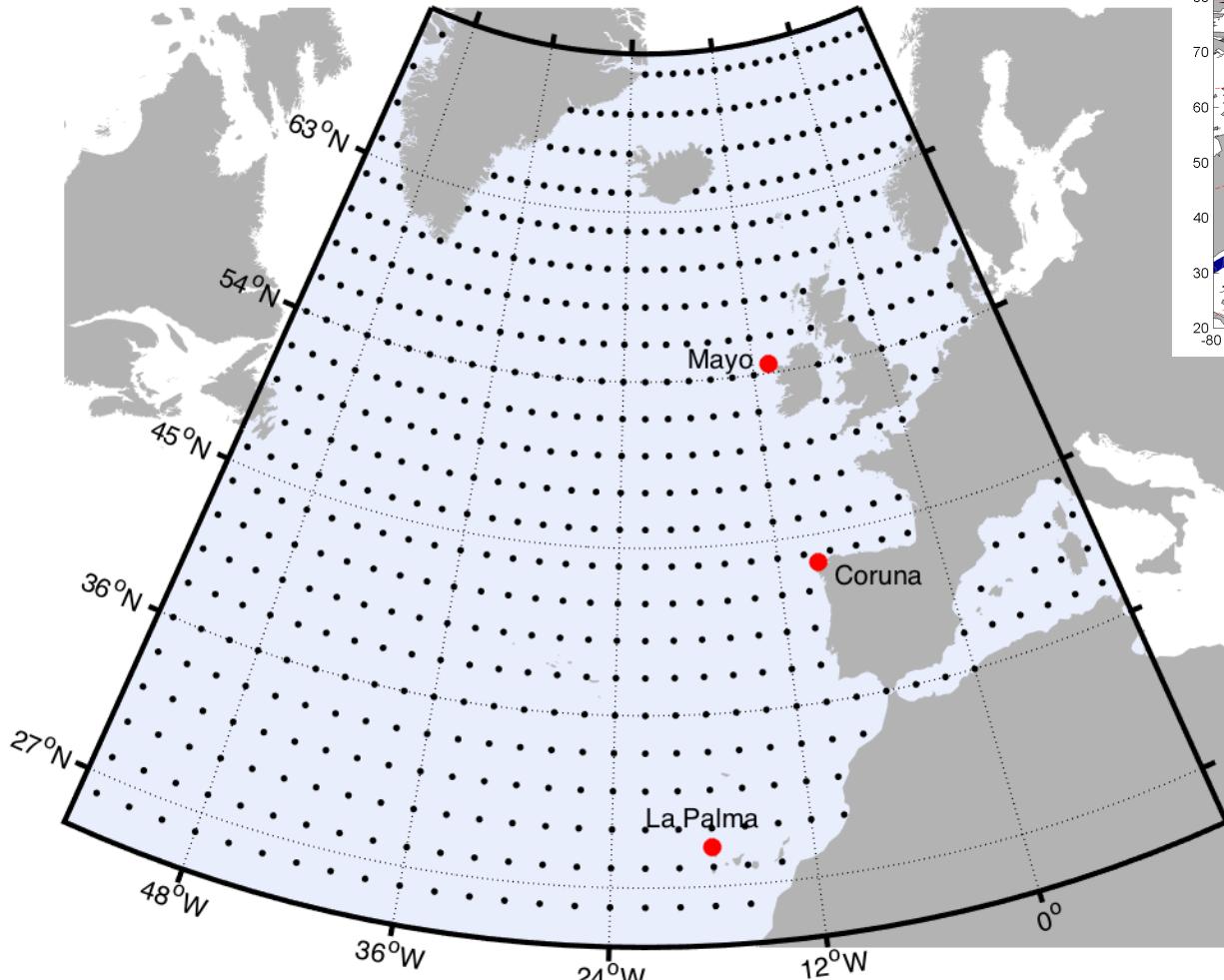
$p_i$  = occurrence probability of  $WT_i$   
 $p_1 + p_2 + p_3 + p_4 = 1$

$N$  = number of block maxima ;  $\theta_i$  = extremal index

$$F_S(H) = F_1(H)^{Np_1\theta_1} \cdot F_2(H)^{Np_2\theta_2} \cdot F_3(H)^{Np_3\theta_3} \cdot F_4(H)^{Np_4\theta_4}$$



# Study Locations - Predictor



(Perez et al., O.D. 2014)

SLP, SLPGrd

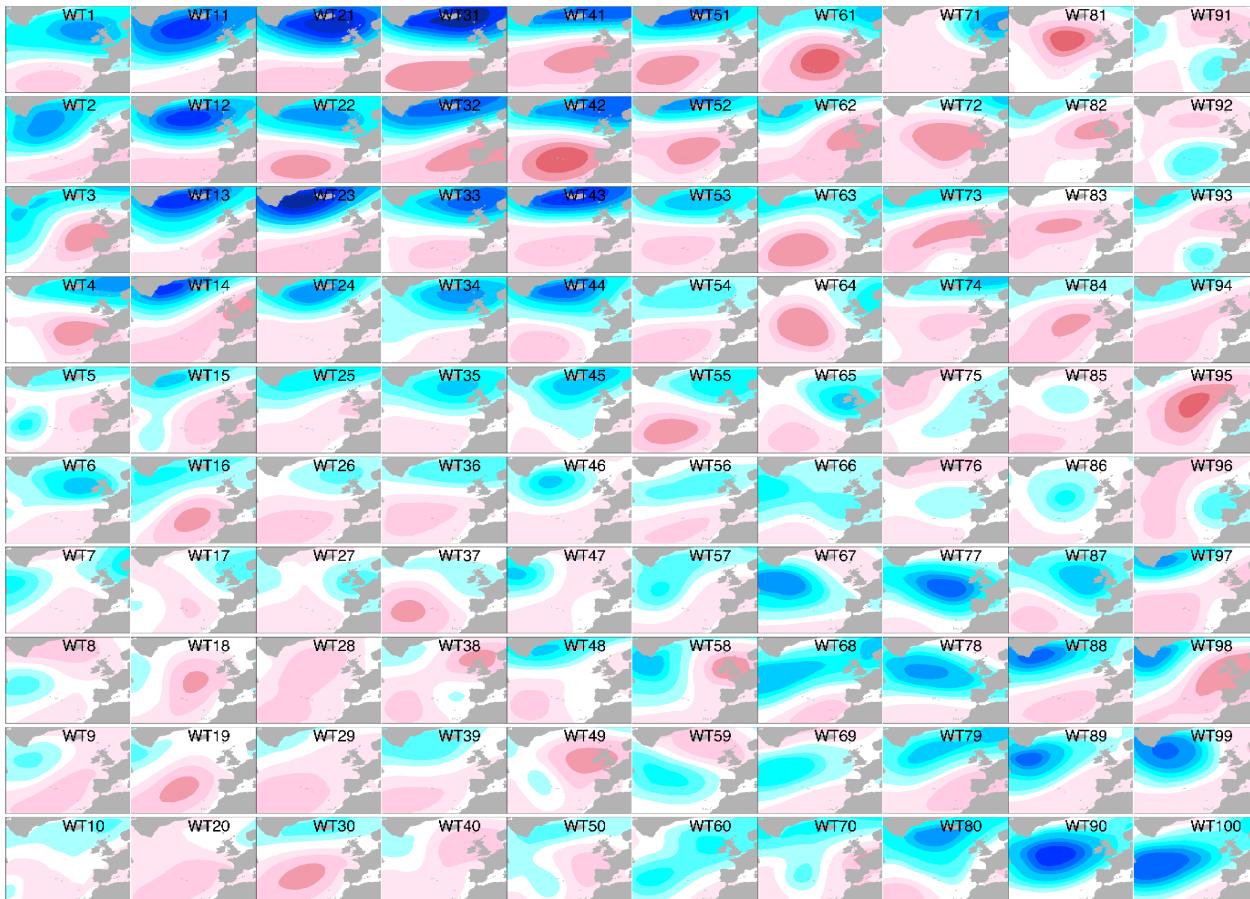
PREDICTOR PRE-PROCESS:  
Historical temporal coverage

(Camus et al., O.D. 2014)

1 day

X days

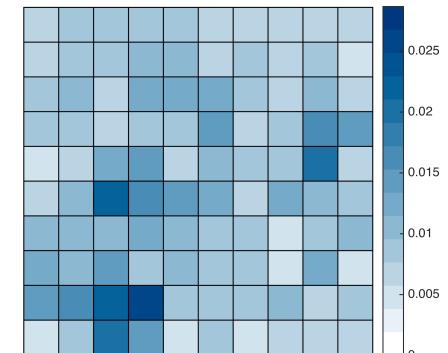
# Weather Types Classification



960 970 980 990 1000 1010 1020 1030 1040 1050 1060

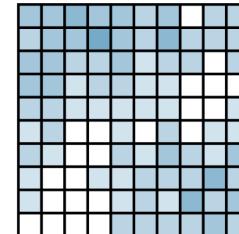
SLP (hPa)

Annual probability

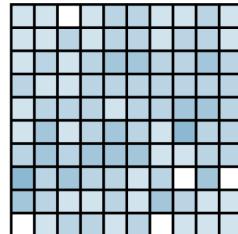


Seasonal probability

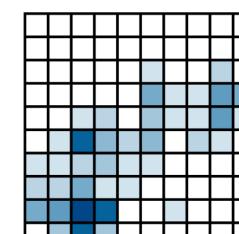
DJF



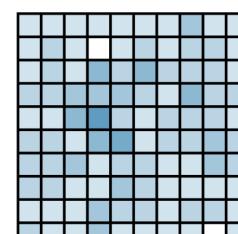
MAM



JJA



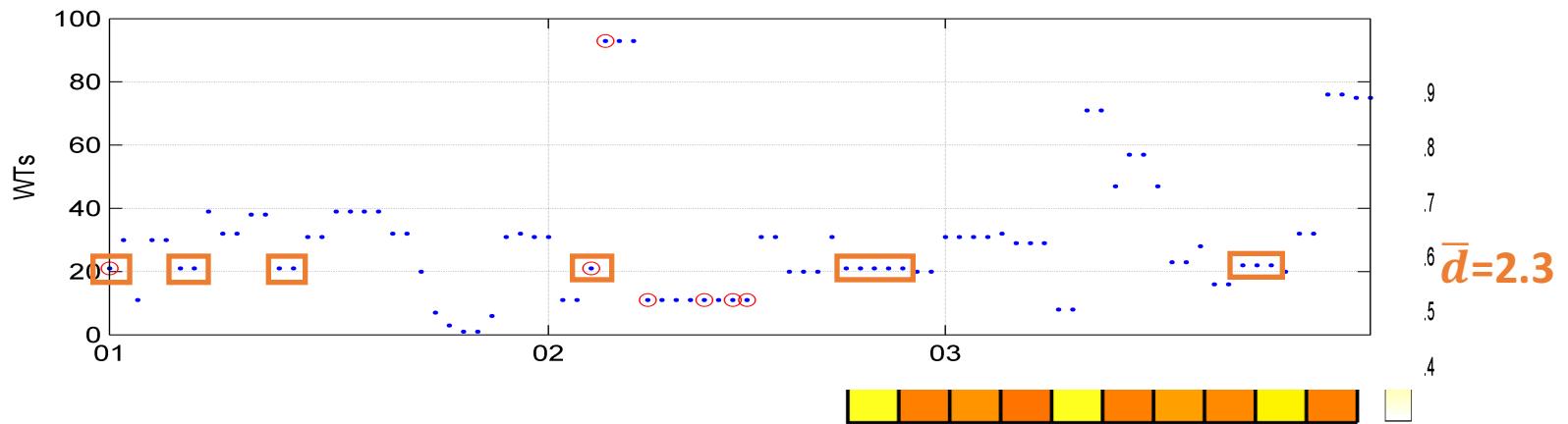
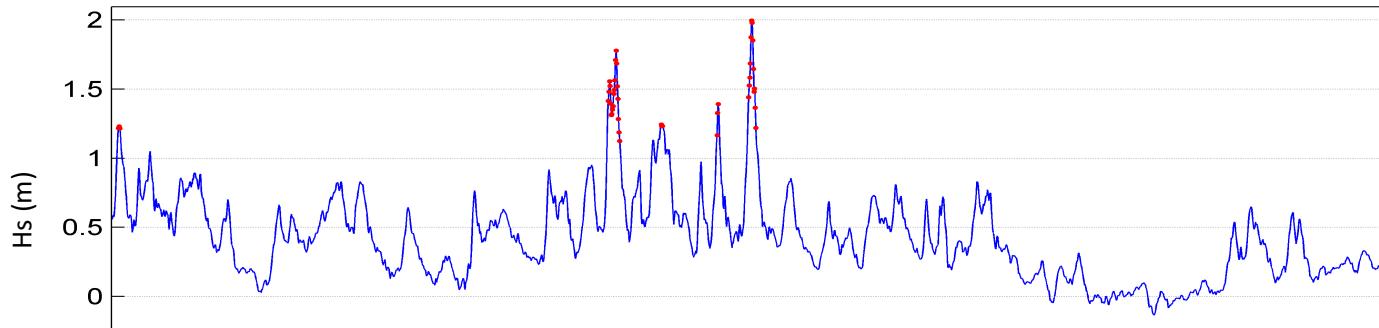
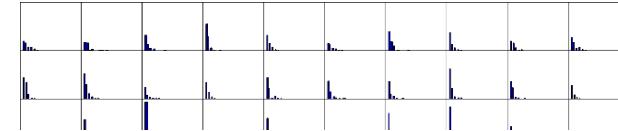
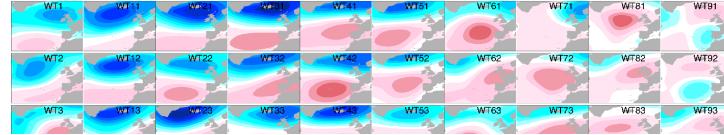
SON



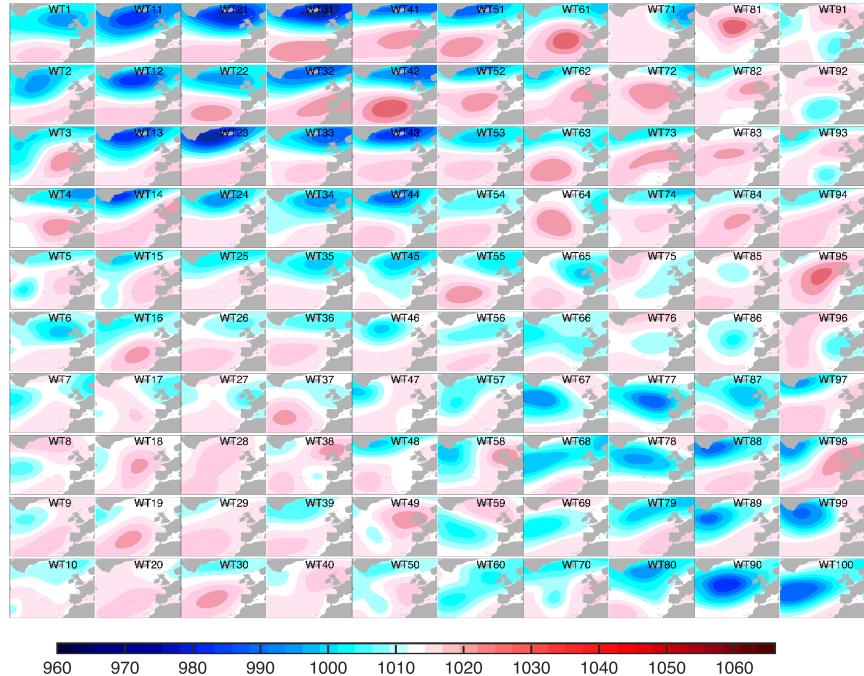
# Climate-related Extremal Index

$$F_y^{Max}(y) = F_y(y)^N \cdot \theta$$

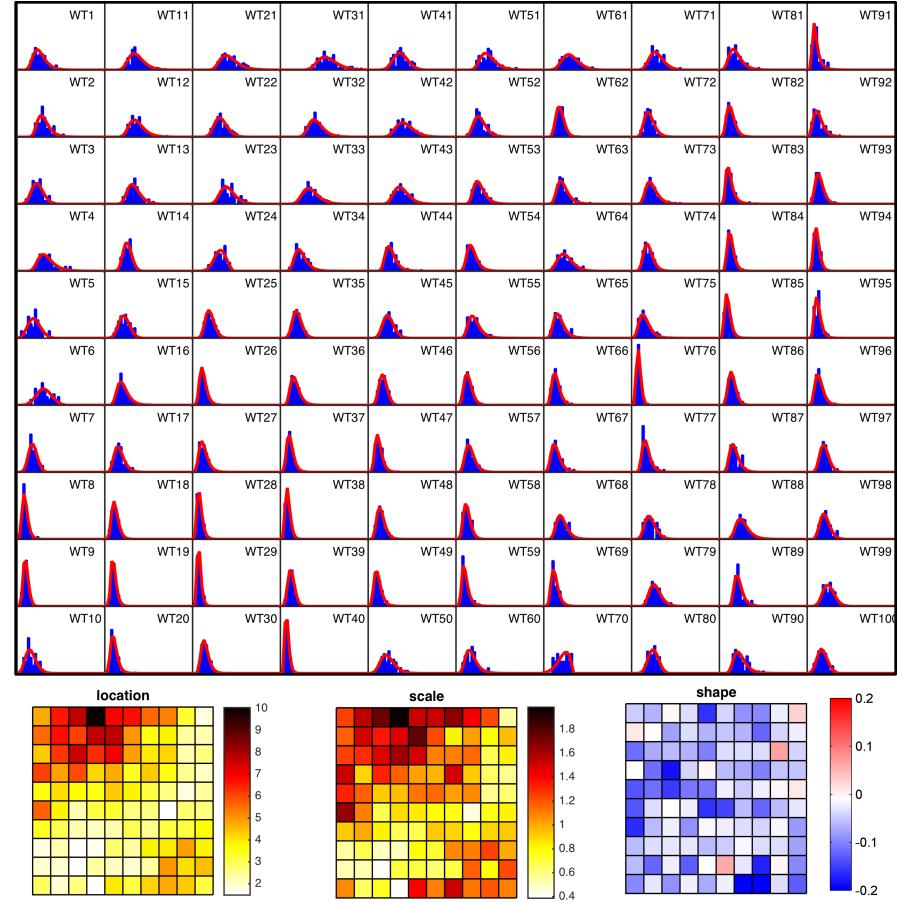
Duration histograms



# GEV distribution associated to each WT



$$F(y) = \exp \left\{ - \left[ 1 + \xi \left( \frac{y - \mu}{\psi} \right) \right]^{-\frac{1}{\xi}} \right\}$$



$\mu$

$\psi$

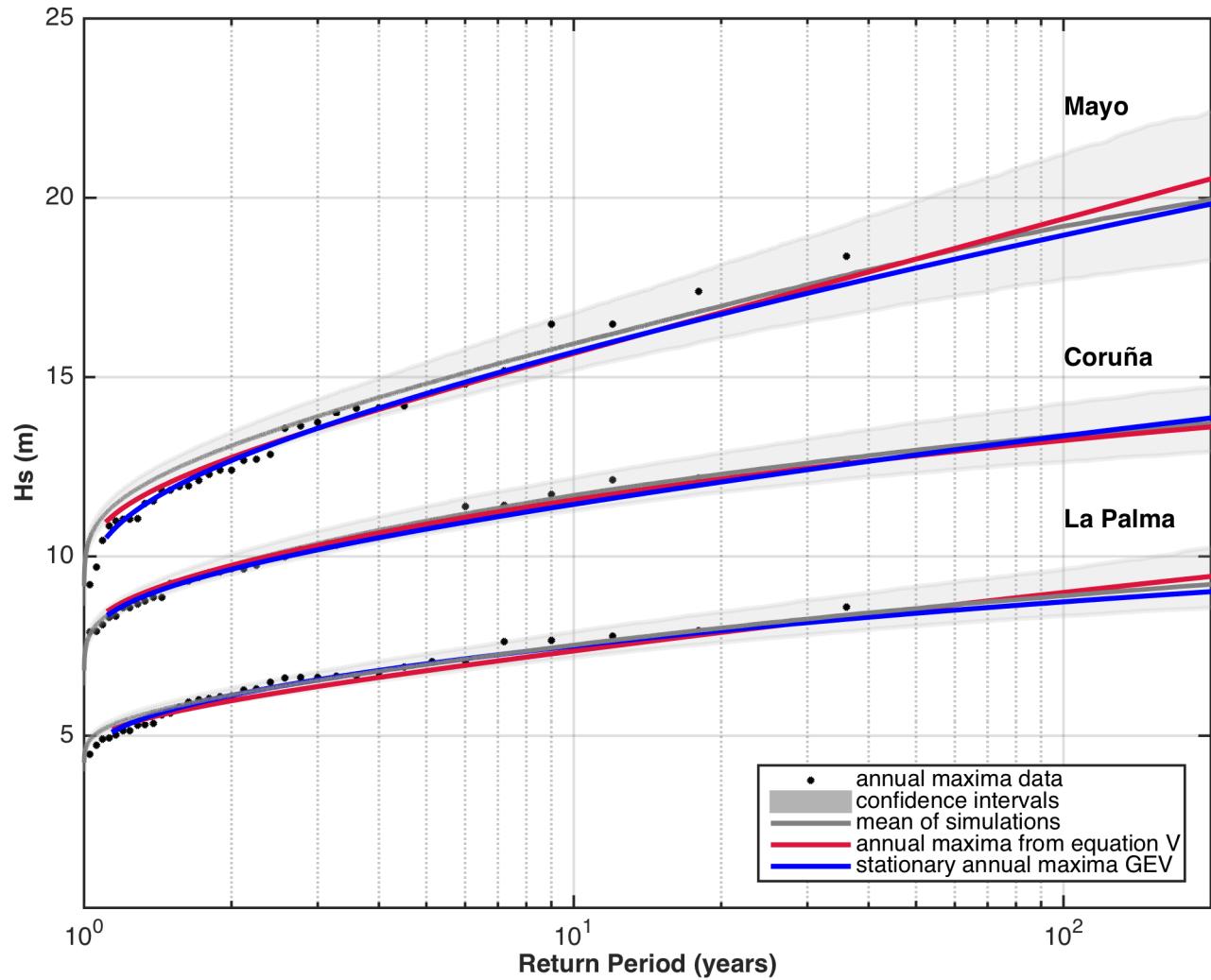
$\xi$

Wave hindcast from Perez et al. 2015

# Annual maxima

$$F(y) = \prod_{i=1}^{N_{wt}} F_i(y)^{N \cdot P_i \cdot \theta_i}$$

$N = 365$   
 $P_i$  = annual probability  
 $P_i, \{i = 1, \dots, N_{wt}\}$



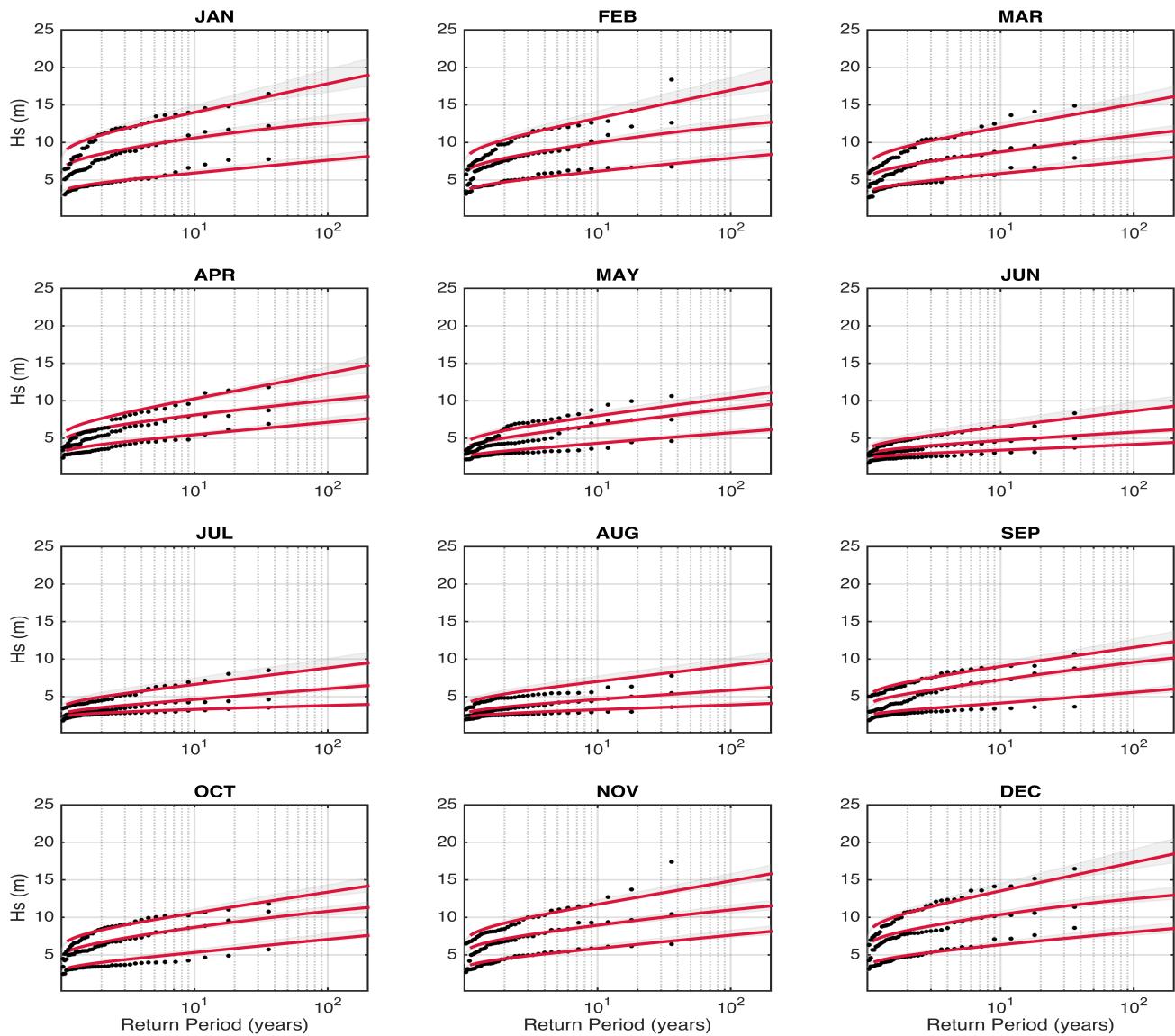
# Monthly maxima

$$F(y) = \prod_{i=1}^{Nwt} F_i(y)^{N \cdot P_i \cdot \theta_i}$$

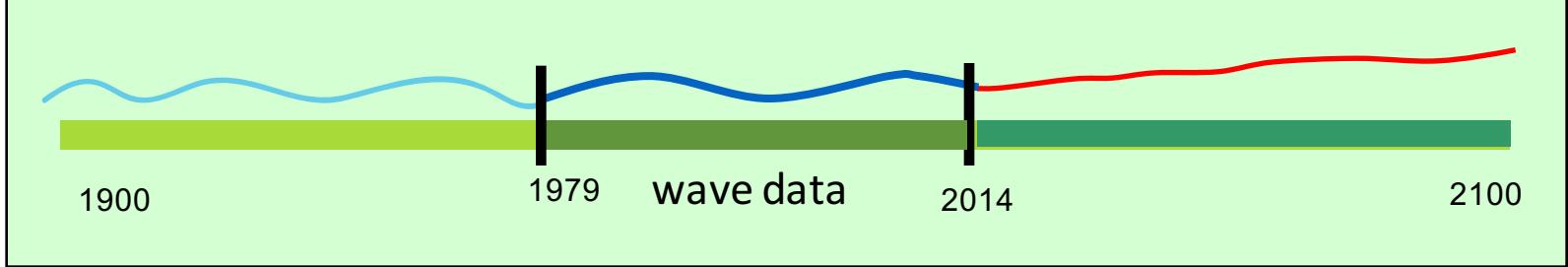
$N = 30$

$P_i$  = monthly probability

$P_i, \{i = 1, \dots, Nwt\}$

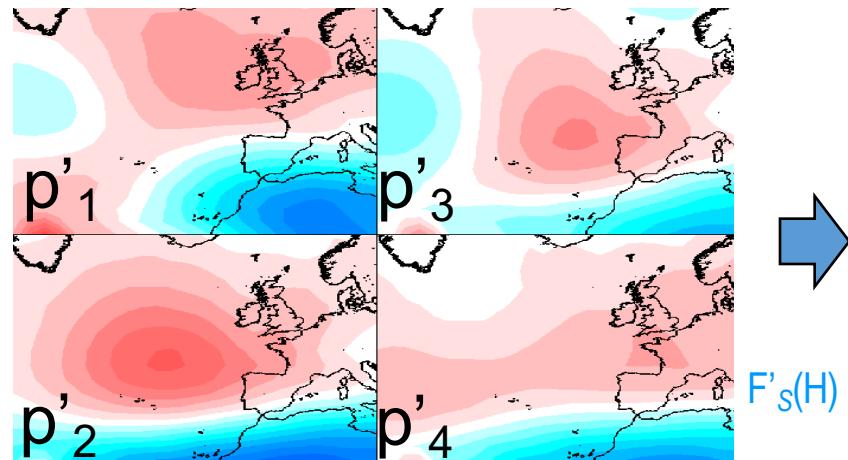


# Assessing Climate Variability



$X' = \text{new predictor}$

$Y = g(X')$



$$p'_1 + p'_2 + p'_3 + p'_4 = 1$$

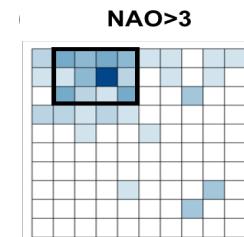
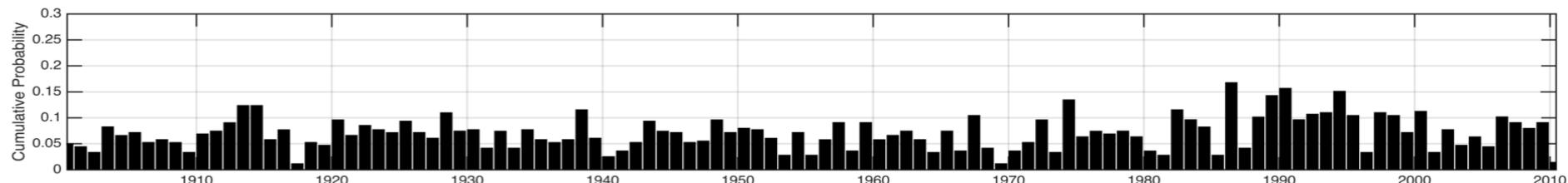
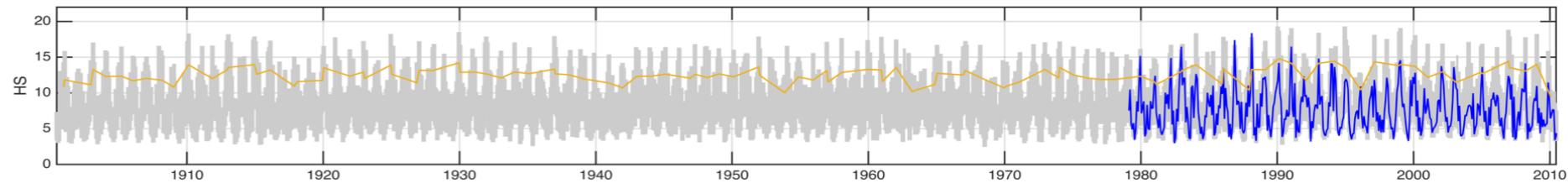
$$F_s(H) = F_1(H)^{Np'_1\theta'_1} \cdot F_2(H)^{Np'_2\theta'_2} \cdot F_3(H)^{Np'_3\theta'_3} \cdot F_4(H)^{Np'_4\theta'_4}$$

# Assessing Climate Variability

20CR atmospheric reanalysis (Compo et al., 2011)



Monthly HS maxima



# Conclusions

- A statistical downscaling model based on **weather types** is able to reproduce the **distribution of maxima significant wave height for different time periods**.
- The **non-stationarity** is introduced in the model by means of changes on the occurrence probability of the associated weather types.
- An example with the 20<sup>th</sup> century atmospheric reanalysis reveals the **importance of large scale patterns** such the NAO on the recorded wave height maxima.

## Acknowledgement

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# An extreme value model for maximum wave heights based on weather types

*Thank you for your attention!*



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# Weather Types Regression-Guided Classification

$$X_i(x) = \{SLP(x), SLPG(x)\}, \quad i=1, \dots, n$$

$$X_i(x) = EOF_i \cdot PC_i + \dots + EOF_d \cdot PC_d,$$

$$X_{EOF} = \{PC_1, \dots, PC_d\}$$

$$Y = X_{EOF} \cdot B + E$$

$$\hat{Y} = X_{EOF} \cdot B$$

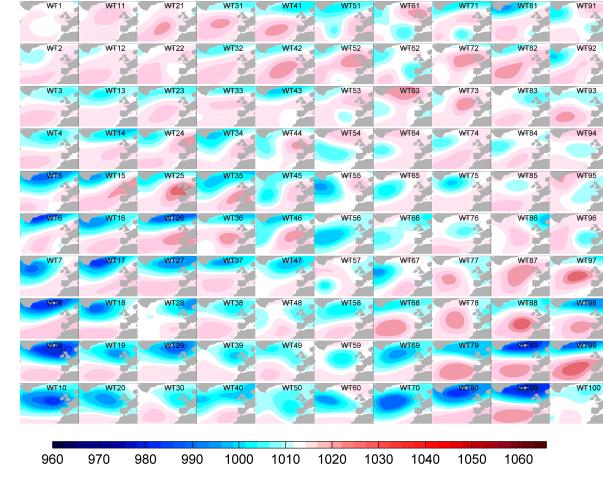
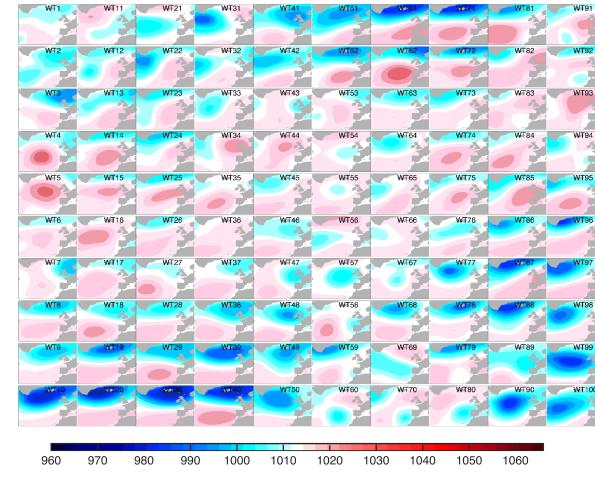
K-Means

$$Z = [(1 - \alpha) \cdot X_{EOF} + \alpha \cdot \hat{Y}];$$

Mayo  $\alpha = 0.3$

La Palma  $\alpha = 0.2$

Coruña  $\alpha = 0.6$



SLP (hPa)

Wave data from Perez et al. (2015)

$N_{WT} = 100$

Cannon et. al (2012)  
Camus et al. OD (submitted)