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Measurement of Ocean Waves with RADARSAT-2 Fully Polarimetric SAR Image

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Conclusions







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Measurement of Ocean Waves from Space

Introduction

Need 1st guess wave spectrum from wave model or wind vector by scatterometer

SAR

Hasselmann et al.(1991) Plant et al.(1997) Mastenbroek et al. (2004) Susanne Lehner et al. (2004) Schulz-Stellenfleth et al. (2007) Li et al. (2009) JGR & IJRS Validated and retrieved for airborne C- and Xband AT-InSAR.

InSAR

Vachon et al.(1999) He et al.(2003) Zhang et al.(2009)

IEEE TGRS & JGR



Spaceborne PolSAR measure ocean waves?

Zhang Biao, Will Perrie and Yijun He (2009), Remote sensing of ocean waves by along-track interferometric synethtic aperture radar, *J. Geophys. Res.*, 114, C10015, doi:10.1029/2009JC005310.





Radar Band	C-band		
Radar Center Frequency (GHz)	5.40		
Pulse Repetition Frequency (Hz)	2769.3		
Satellite Height (km)	795.8		
Platform Velocity (km/s)	7.46		
Track Angle (deg)	10.91		
Slant range to velocity ratio (s)	137.6		
Acquisition Type	Fine Quad Polarization		
Polarizations	HH VV HV VH		
Sampled Pixel Spacing (m)	4.73		
Sampled Line Spacing (m)	4.79		

Table1. RADARSAT-2 fully polarimetric image parameters



NDBC Buoy Observations



Image	Acquired	Buoy time	Image central	Buoy site	Wind	Wind
id	time		site		Speed	direction
	(UTC)				(m/s)	(deg)
1	02:25:04 11 Jan 2009	02:50:00 11 Jan 2009	46°04'06"N 131°02'22"W	46°03'00"N 131°01'12"W	9.0	240
2	14:30:58 18 Jan 2009	14:50:00 18 Jan 2009	45°57'43"N 125°39'18"W	45°54'28"N 125°45'37"W	3.7	97
3	02:09:26 25 Feb 2009	01:50:00 25 Feb 2009	35°44'43"N 121°55'42"W	35°44'29"N 121°53'03"W	5.3	321
4	05:47:58 28 Feb 2009	05:50:00 28 Feb 2009	51°07'18"N 178°53'10"W	51°09'17"N 179°00'02"W	4.0	270
5	14:39:15 17 Mar 2009	14:50:00 17 Mar 2009	46°07'05"N 124°33'25"W	46°08'37"N 124°30'37" W	7.7	246
6	14:31:05 22 Aug 2009	14:50:00 22 Aug 2009	46°05'06"N 124°30'01"W	46°08'37"N 124°30'37" W	3.0	20

Table2. RADARSAT-2 fully polarimetric SAR and NDBC buoys.



NDBC Buoy Observations



3-meter discus buoy



6-meter NOMAD buoy



Because max. sensitivities to wave slopes are obtained using linear polarizations \rightarrow the ellpticity χ is set to zero [*Schuler and Lee*, 1995], and the backscatter cross section is

$$\sigma(0,\psi) = \frac{1}{4} (\underline{\sigma_{hh}} + \underline{\sigma_{vv}}) \cdot [1 + \cos^2(2\psi)] + \frac{1}{2} (\sigma_{hh} - \sigma_{vv}) \cos(2\psi) + (\overline{\sigma_{hv}}) + \frac{1}{2} \operatorname{Re}(\sigma_{hhvv}) \sin^2(2\psi)$$
(2)

Wave slopes in the azimuth and range directions

Via linear modulation theory, ocean surface elevation ξ and variations of local backscatter cross section $\sigma(\mathbf{r},t)$ may be represented as

$$\xi(\mathbf{r},t) = \sum_{k} \xi_{k} \exp(\mathbf{k} \cdot \mathbf{r} - \omega t) + c.c$$
(5)

$$\sigma_{pp}(\mathbf{r},t) = \overline{\sigma}_{pp} \left\{ 1 + \left[\sum_{k} T_{kpp}^{R} \xi_{k} \exp i(\mathbf{k} \cdot \mathbf{r} - \omega t) + c.c \right] \right\}$$
(6)
$$\int_{T_{kpp}} T_{kpp}^{t} + T_{k}^{h} + T_{kpp}^{p} + T_{k}^{rb}$$

For single-Pol SAR, T_k^{ν} (+) T_{kpp}^{p} (-)

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$$\frac{\Delta \sigma_{hh}(\mathbf{r},t)}{\overline{\sigma}_{hh}} = \sum_{k} T_{khh}^{t} \xi_{k} \exp[i(\mathbf{k} \cdot \mathbf{r} - \omega t)] + c_{1} + R$$
(8)

$$\frac{\Delta \sigma_{vv}(\mathbf{r},t)}{\overline{\sigma}_{vv}} = \sum_{k} T_{kvv}^{t} \xi_{k} \exp[i(\mathbf{k} \cdot \mathbf{r} - \omega t)] + c_{2} + R$$

(7)

$$\begin{array}{c} \textbf{Methodc} \ T_{\mathbf{k}}^{p} = -\frac{ik_{x}}{A_{0}} \left[\left(1 + \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \cos(2\varphi) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 - \left(\frac{1 + \sin^{2}\theta}{\cos^{2}\theta} \right)^{2} \right) \\ + \left(1 -$$

only modulation transfer for tilt + polarization orientation angle depend on polarization \rightarrow

$$\frac{\Delta \sigma_{vv}(\mathbf{r},t)}{\overline{\sigma}_{vv}} - \frac{\Delta \sigma_{hh}(\mathbf{r},t)}{\overline{\sigma}_{hh}} = \sum_{k} (T_{kvv}^{t} - T_{khh}^{t}) \xi_{k} \exp i(\mathbf{k} \cdot \mathbf{r} - \omega t) + c_{1}$$
(10)

$$\frac{\Delta\sigma_{\psi\psi}(\mathbf{r},t)}{\bar{\sigma}_{\psi\psi}} - \frac{\Delta\sigma_{\psi}(\mathbf{r},t)}{\bar{\sigma}_{\psi\psi}} = \sum_{k} (T_{k\psi\psi}^{t} + T_{k\psi\psi}^{p} - T_{kvv}^{t})\xi_{k} \exp i(\mathbf{k}\cdot\mathbf{r} - \omega t) + c_{2}$$
(11)

When
$$\psi = 0$$
 then $T_{k\nu\nu}^t = ik_x \frac{4 - 0.5(1 - \sin^2 \theta)}{\tan \theta (1 - \sin^2 \theta)}$ $T_{khh}^t = ik_x \frac{4 - 0.5(1 + \sin^2 \theta)}{\tan \theta (1 + \sin^2 \theta)}$ (12)

Wave slopes in the azimuth and range directions

With some algebra we get

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$$\frac{\Delta \sigma_{vv}}{\overline{\sigma}_{vv}} - \frac{\Delta \sigma_{hh}}{\overline{\sigma}_{hh}} = -\frac{8 \tan \theta}{1 + \tan^2 \theta} \frac{\partial \xi}{\partial x}$$
(13)
$$\frac{\Delta \sigma_{\psi\psi}}{\overline{\sigma}_{\psi\psi}} - \frac{\Delta \sigma_{vv}}{\overline{\sigma}_{vv}} = a \frac{\partial \xi}{\partial x} + b \frac{\partial \xi}{\partial y}$$
(14)

where $\partial \xi / \partial x$ and $\partial \xi / \partial y$ are wave slopes in the range and azimuth directions.

$$a = \frac{a_2}{a_0} - a_3, \ b = \frac{a_1}{a_0} \qquad a_1 = -\left[\left\{1 + \left[\frac{(1 + \sin^2\theta)}{(1 - \sin^2\theta)}\right]^2\right\} \cos(2\psi) + \left\{1 - \left[\frac{(1 + \sin^2\theta)}{(1 - \sin^2\theta)}\right]^2\right\} \\ a_0 = \frac{1}{4}\left\{1 + \left[\frac{(1 + \sin^2\theta)}{(1 - \sin^2\theta)}\right]^2\right\} [1 + \cos^2(2\psi)] \qquad -2\left[\frac{(1 + \sin^2\theta)}{(1 - \sin^2\theta)}\right] \cos(2\psi) \left[\frac{\sin(2\psi)}{\sin\theta} - \frac{2\sin^2\theta}{1 - 8\sin^2\theta + 8\sin^4\theta} \cos(2\psi) + \frac{1 + 2\tan^2\theta}{2}\sin^2(2\psi) - a_2 = \left[\frac{2\tan\theta}{\sin^2\theta\cos^2\theta} [1 + \cos^2(2\psi)] - \frac{4\tan^3\theta}{\sin^2\theta}\cos(2\psi) + \frac{2\tan^3\theta}{\sin^2\theta}\sin^2(2\psi)\right] + \frac{1 + 2\tan^2\theta}{\sin^2\theta}\sin^2(2\psi) = \frac{1 + 2\tan^2\theta}{\sin^2\theta}\sin^2\theta}\sin^2(2\psi) = \frac{1 + 2\tan^2\theta}{\sin^2\theta}\sin^2\theta}\sin^2\theta$$

2 Wave slopes in the azimuth and range directions

Average wave height of dominant wave can be estimated with rms slope:

$$S_{rms} = [(\langle S_{az} \sin \Phi \rangle)^2 + (\langle S_r \cos \Phi \rangle)^2]^{1/2}$$
(15)

$$S_{az} = \partial \xi / \partial y$$
 $S_r = \partial \xi / \partial x$ (16)

$$\tan(S_{rms}) = H_d / (\lambda_d / 2) \tag{17}$$





Figure 1. A C-band, VV polarization image of northwest of Morro Bay, California acquired by RADARSAT-2 at 02:09 on February 25, 2009 UTC.

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RADARSAT-2 fully polarized images





Figure 2. A C-band, VV polarization image of northwest of Tillamook Bay, OR acquired by RADARSAT-2 at 14:30 on January 18, 2009 UTC.

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RADARSAT-2 fully polarized images

Case Studies





Figure 3. A C-band, VV polarization image of west of Columbia River Mouth acquired b y RADARSAT-2 at 14:31 on August 22, 2009 UTC.

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RADARSAT-2 fully polarized images





Figure 4. A C-band, VV polarization image of an area west of Aberdeen, WA acquired by RADARSAT-2 at 02:25 on January 11, 2009 UTC.

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Wave slope spectrum by <u>SAR</u> for west of Aberdeen at 02:05 Jan. 11, 2009



